

Advance Q-Learning

CMPT 729 G100

Jason Peng

Overview

- Nonstationary Targets
- Overestimation
- Model Architecture

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- Nonstationary Targets → Target Networks
- Overestimation
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Moving Target

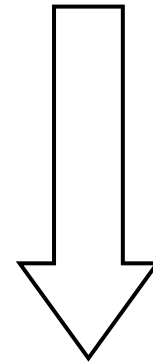
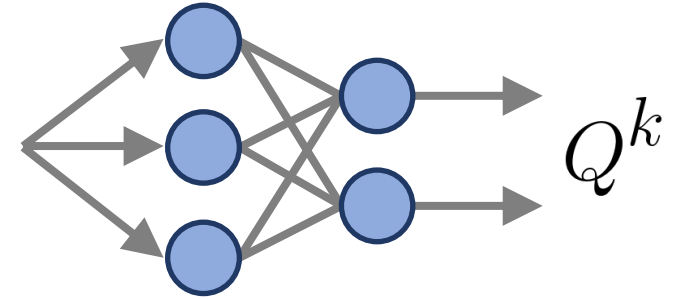
$$Q^{k+1} = \arg \min_Q \mathbb{E}_{(\mathbf{s}_i, \mathbf{a}_i, r_i, \mathbf{s}'_i) \sim \mathcal{D}} \left[\underline{y_i} - Q(\mathbf{s}_i, \mathbf{a}_i) \right]^2$$

$$y_i = r_i + \gamma \max_{\mathbf{a}'} \underline{Q^k}(\mathbf{s}', \mathbf{a}')$$

- Target values change every iteration
- Can lead to unstable learning dynamics

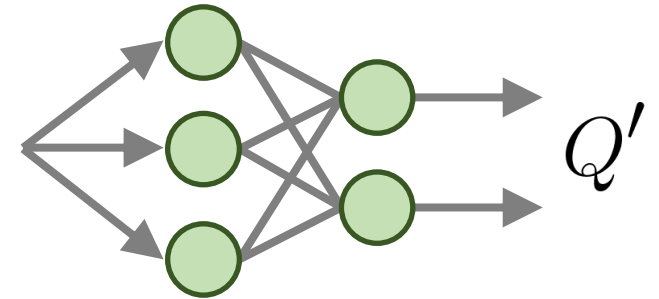
Target Network

$$y_i = r_i + \gamma \max_{\mathbf{a}'} Q^k(\mathbf{s}', \mathbf{a}')$$



$$y_i = r_i + \gamma \max_{\mathbf{a}'} \underline{Q}'(\mathbf{s}', \mathbf{a}')$$

target network



Target Network

$$Q^{k+1} = \arg \min_Q \mathbb{E}_{(\mathbf{s}_i, \mathbf{a}_i, r_i, \mathbf{s}'_i) \sim \mathcal{D}} \left[\underline{y_i} - Q(\mathbf{s}_i, \mathbf{a}_i) \right]^2$$

$$y_i = r_i + \gamma \max_{\mathbf{a}'} \underline{Q'}(\mathbf{s}', \mathbf{a}')$$

- Target network is a delayed copy of the Q-function
- Every m iterations, copy parameters from Q-function to target network
- Works well in practice to stabilize Q-learning

Deep Q-Network (DQN)

Experience Replay + Target Network



Human-Level Control Through Deep Reinforcement Learning
[Mnih et al. 2015]

Target Network

$$Q^{k+1} = \arg \min_Q \mathbb{E}_{(\mathbf{s}_i, \mathbf{a}_i, r_i, \mathbf{s}'_i) \sim \mathcal{D}} \left[\underline{y_i} - Q(\mathbf{s}_i, \mathbf{a}_i) \right]^2$$

$$y_i = r_i + \gamma \max_{\mathbf{a}'} \underline{Q'}(\mathbf{s}', \mathbf{a}')$$

- Every m iterations, copy parameters from Q-function to target network
- ✓ Works well in practice to stabilize Q-learning
- ✗ Abrupt changes to target values every m iterations
- ✗ Can cause some unstable learning dynamics

Polyak Averaging

- Initialize target network with the *same* parameters a Q-function
- Every iteration, update target network:

$$\theta^{Q'} \leftarrow \alpha \theta^{Q^k} + (1 - \alpha) \theta^{Q'}$$

step size
(e.g. $\alpha = 0.001$)

Polyak Averaging

- Initialize target network with the *same* parameters a Q-function
- Every iteration, update target network:

$$\theta^{Q'} \leftarrow \alpha \theta^{Q^k} + (1 - \alpha) \theta^{Q'}$$

step size
(e.g. $\alpha = 0.001$)

- Smoother changes to target values

Target Network

$$Q^{k+1} = \arg \min_Q \mathbb{E}_{(\mathbf{s}_i, \mathbf{a}_i, r_i, \mathbf{s}'_i) \sim \mathcal{D}} \left[\underline{y_i} - Q(\mathbf{s}_i, \mathbf{a}_i) \right]^2$$

$$y_i = r_i + \gamma \max_{\mathbf{a}'} \underline{Q'(\mathbf{s}', \mathbf{a}')}$$

Slowly moving target network

- Works very well in practice
- Nearly every modern Q-learning algorithms uses some kind of target network

DQN

ALGORITHM: DQN

- 1: $Q^0 \leftarrow$ initialize Q-function
 - 2: $Q' \leftarrow$ initialize target network with parameters from Q^0
 - 3: $\mathcal{D} \leftarrow \{\emptyset\}$ initialize empty replay buffer

 - 4: **for** iteration $k = 0, \dots, n - 1$ **do**
 - 5: Sample trajectory τ according to $Q^k(\mathbf{s}, \mathbf{a})$
 - 6: Store transitions $\{(\mathbf{s}_i, \mathbf{a}_i, r_i, \mathbf{s}'_i)\}$ in replay buffer \mathcal{D}

 - 7: Calculate target values for each sample i :
 $y_i = r_i + \gamma \max_{\mathbf{a}'} Q'(\mathbf{s}'_i, \mathbf{a}')$

 - 8: Update Q-function:
 $Q^{k+1} = \arg \min_Q \mathbb{E}_{(\mathbf{s}_i, \mathbf{a}_i, r_i, \mathbf{s}'_i) \sim \mathcal{D}} [(y_i - Q(\mathbf{s}_i, \mathbf{a}_i))^2]$

 - 9: Update target network:
 $\theta^{Q'} \leftarrow \alpha \theta^{Q^{k+1}} + (1 - \alpha) \theta^{Q'}$
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 - 11: return Q^n
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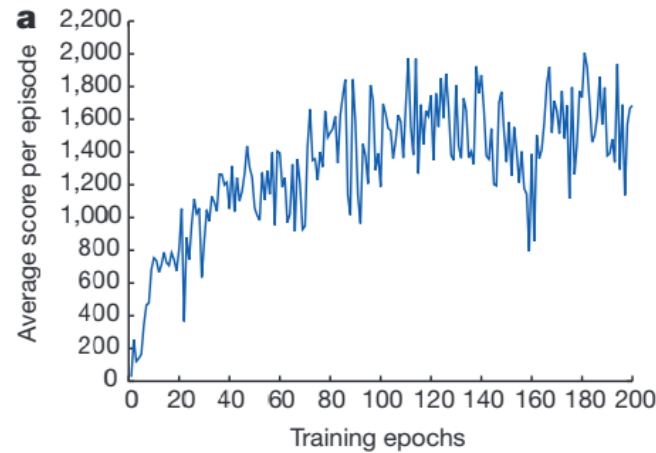
Overview

- Nonstationary Targets → Target Networks
- **Overestimation → Pessimistic Estimates**
- Model Architecture

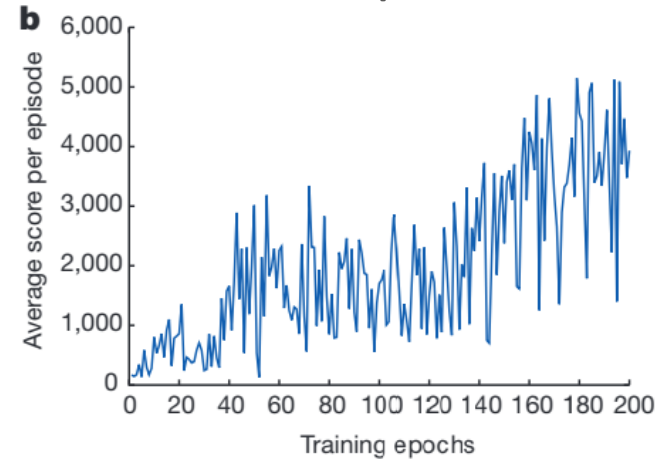
How Accurate is the Q-Function?

Real Score

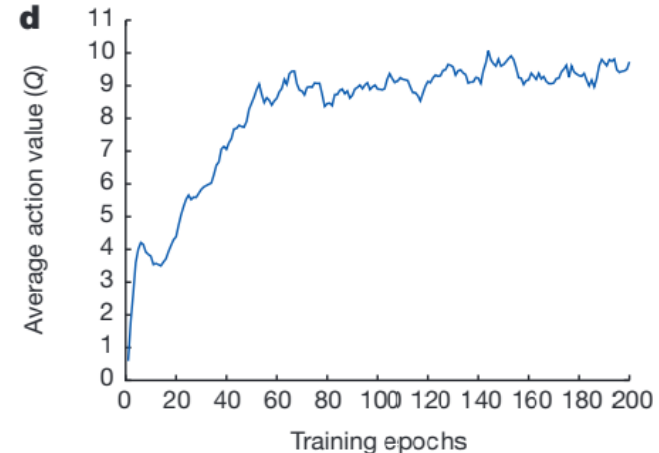
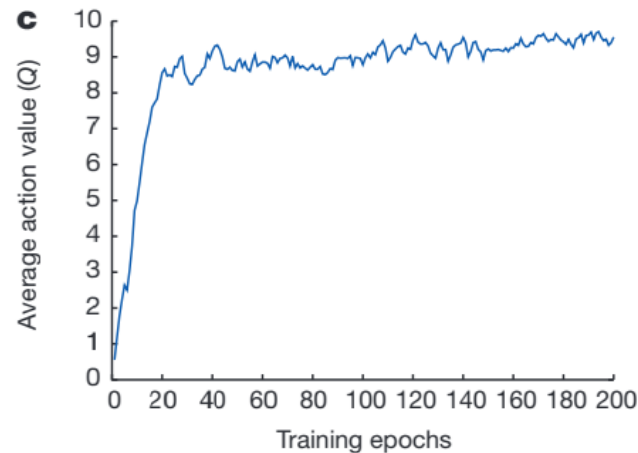
Space Invaders



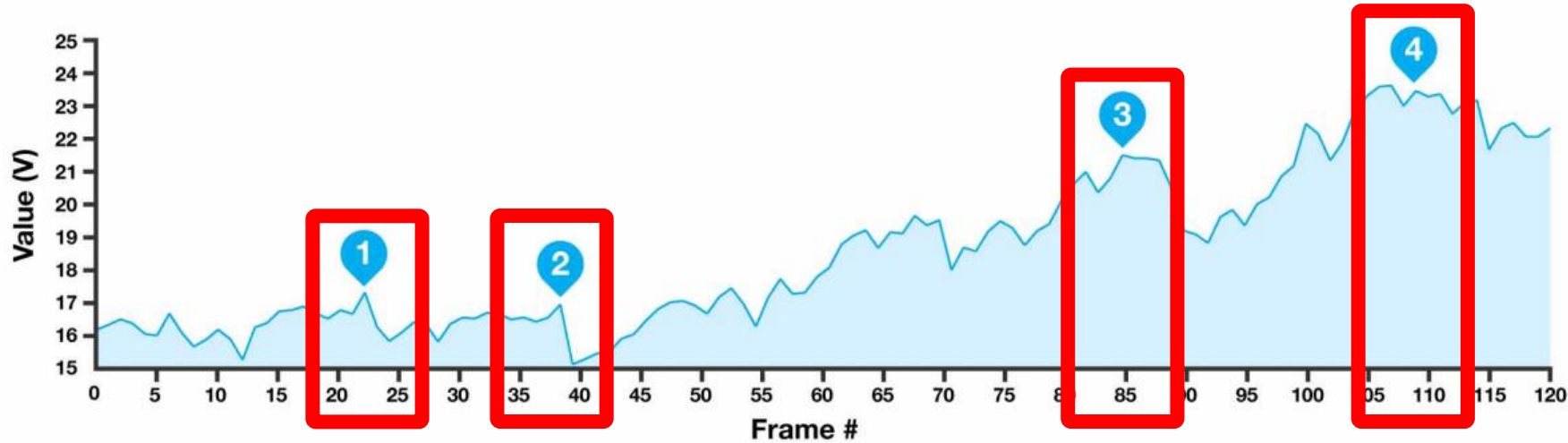
Seaquest



Predicted Value

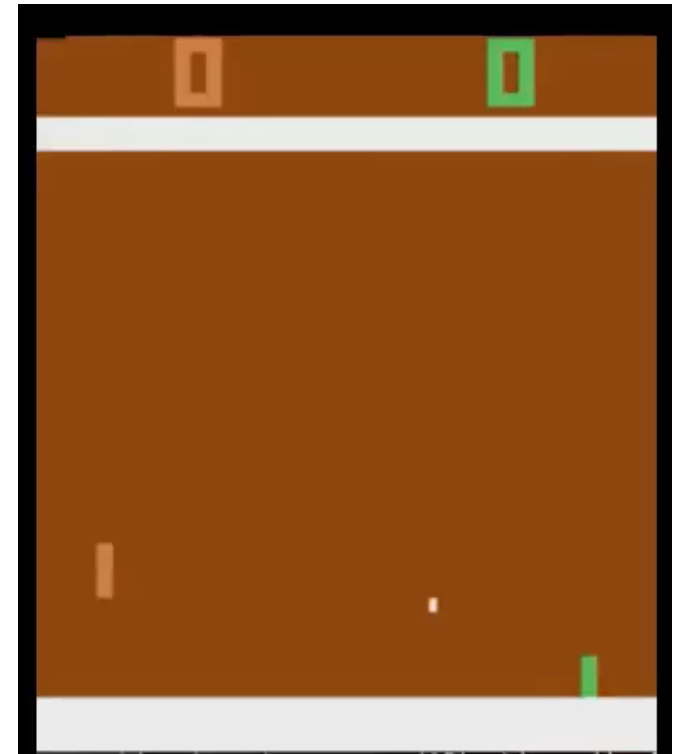
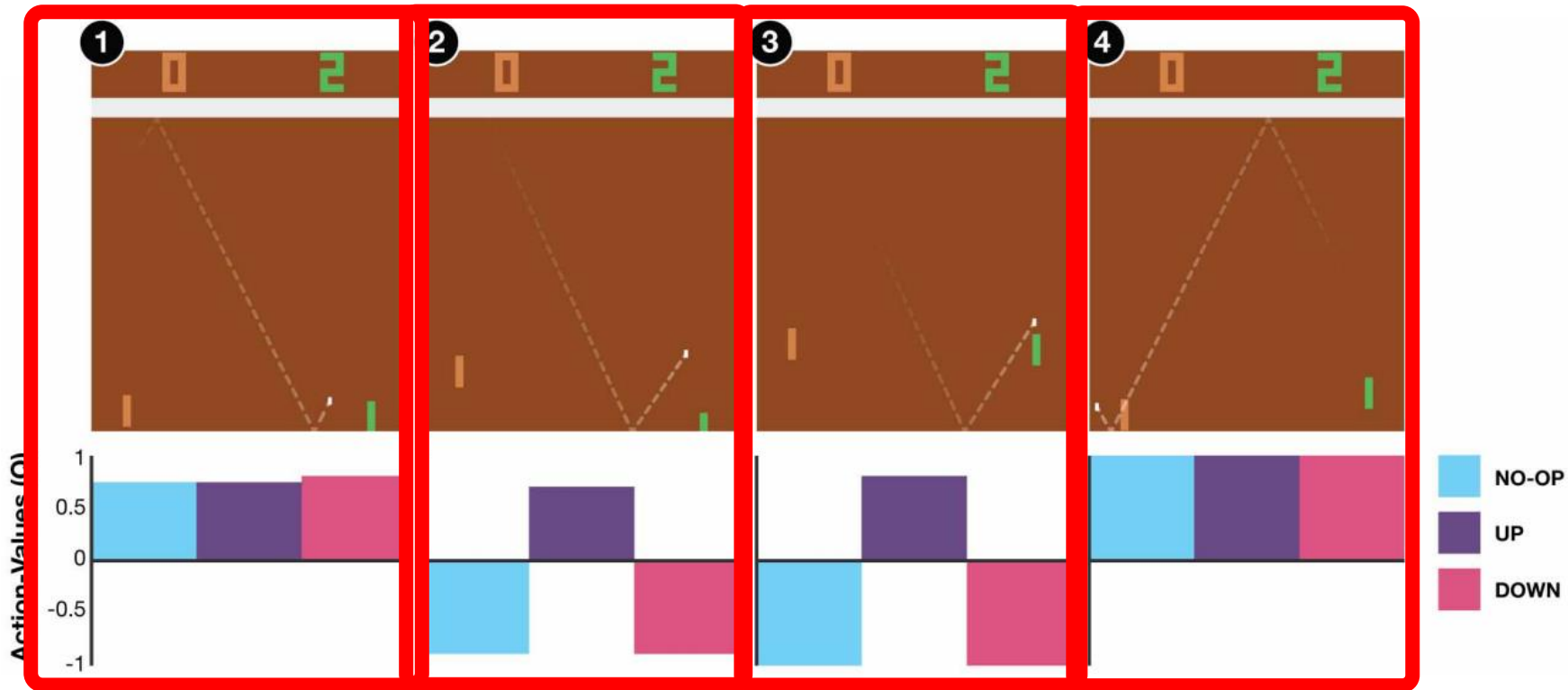


How Accurate is the Q-Function?



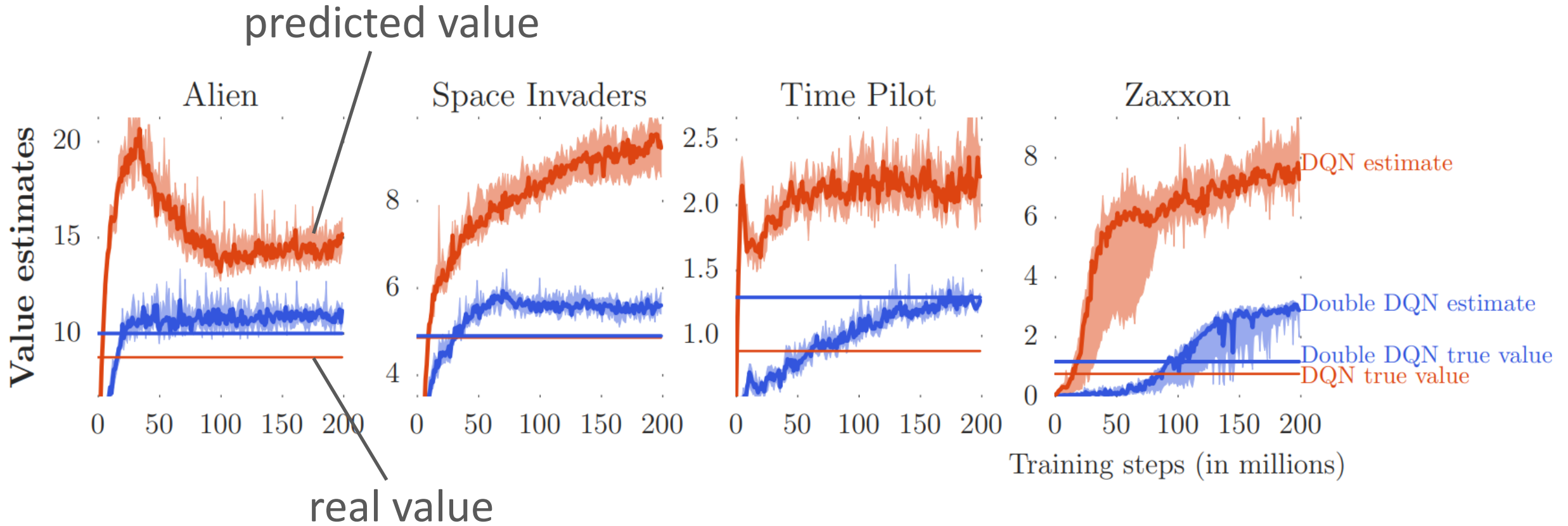
Human-Level Control Through Deep Reinforcement Learning
[Mnih et al. 2015]

How Accurate is the Q-Function?



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Overestimation

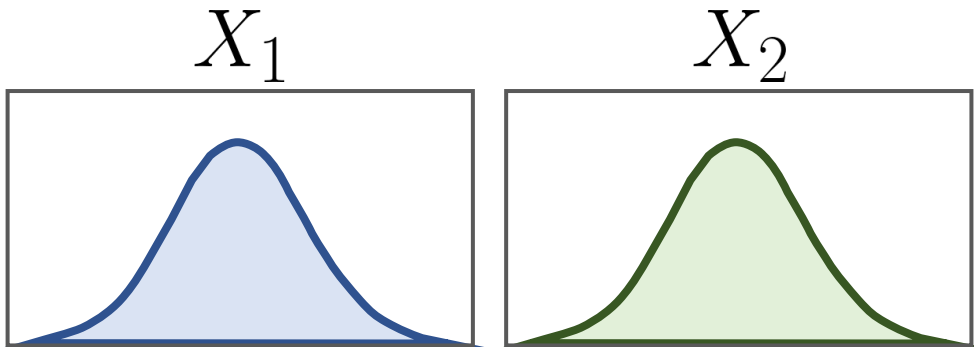


Deep Reinforcement Learning with Double Q-learning
[van Hasselt et al. 2016]

Overestimation

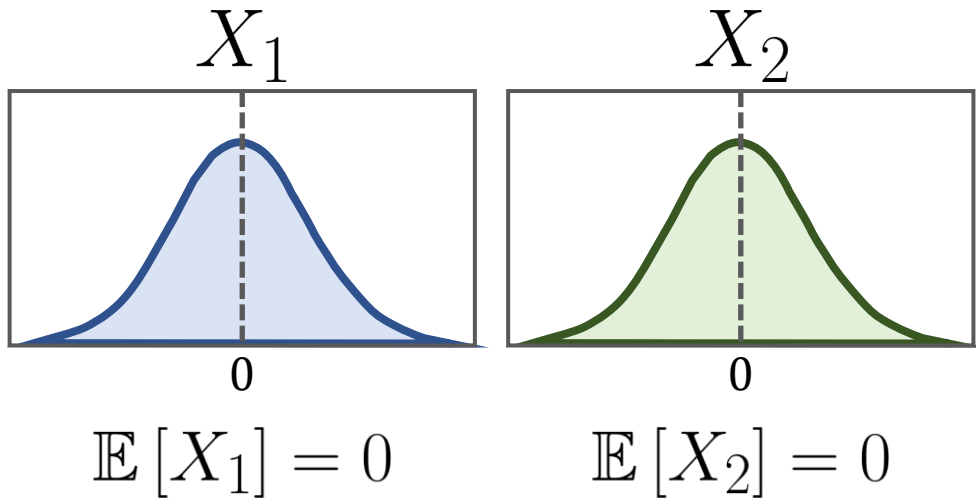
$$y_i = r_i + \gamma \max_{\mathbf{a}'} Q^k(\mathbf{s}', \mathbf{a}')$$

Bias towards positive errors



Overestimation

$$y_i = r_i + \gamma \max_{\mathbf{a}'} Q^k(\mathbf{s}', \mathbf{a}')$$



$$\mathbb{E}[\max(X_1, X_2)] > 0$$

$$p(X_1 > 0) = p(X_2 > 0) = 0.5$$

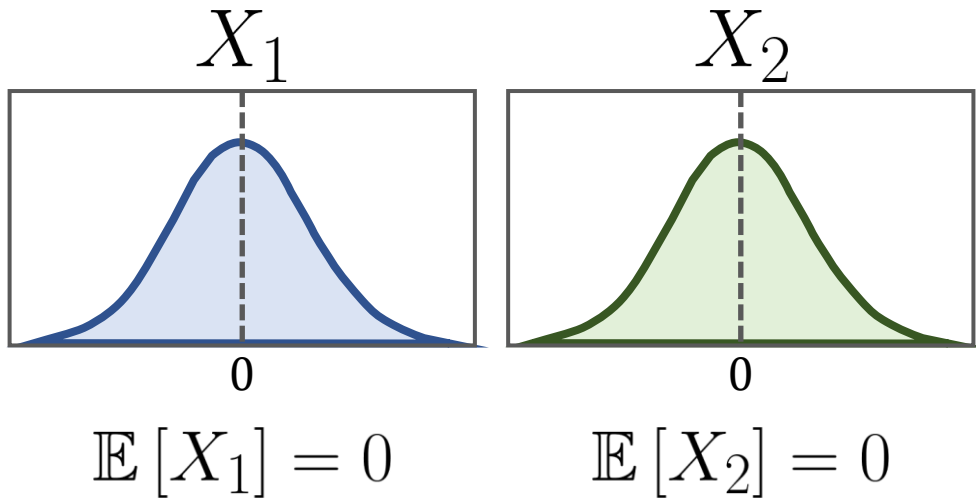
$$p(\max(X_1, X_2) > 0)$$

$$= p(X_1 > 0 \text{ or } X_2 > 0) = \underline{0.75}$$

Overestimation

$$y_i = r_i + \gamma \max_{\mathbf{a}'} \underline{Q^k(\mathbf{s}', \mathbf{a}')}$$

Tends to be noisy



$$\mathbb{E}[\max(X_1, X_2)] > 0$$

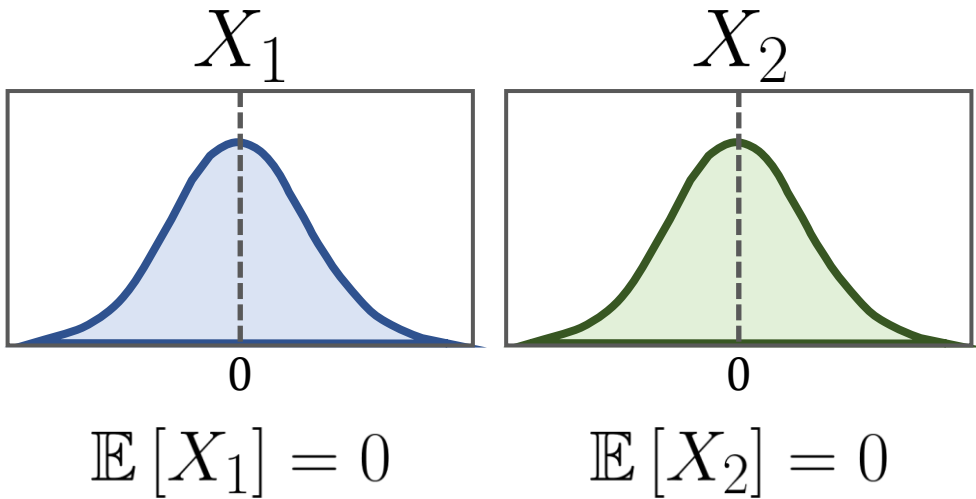
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Overestimation

$$y_i = r_i + \gamma \max_{\mathbf{a}'} Q^k(\mathbf{s}', \mathbf{a}')$$

More likely to *overestimate* next value



$$\mathbb{E}[\max(X_1, X_2)] > 0$$

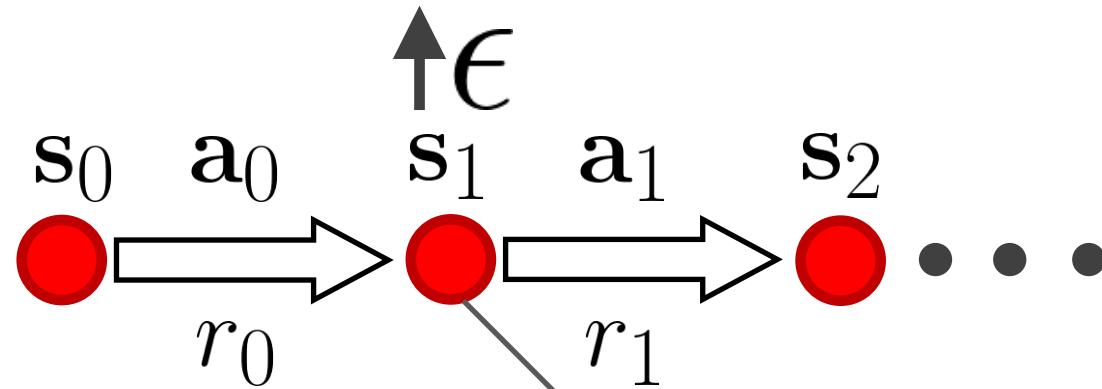
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Overestimation

$$y_i = r_i + \gamma \max_{\mathbf{a}'} Q^k(\mathbf{s}', \mathbf{a}')$$

Bootstrapping can propagate overestimation errors

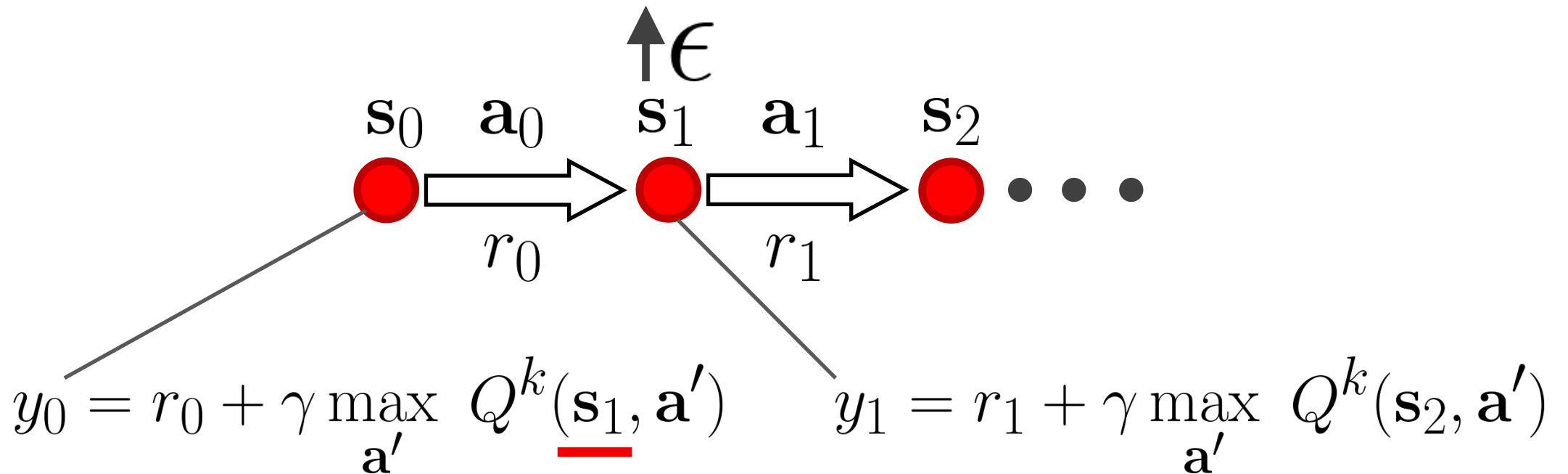


$$y_1 = r_1 + \gamma \max_{\mathbf{a}'} Q^k(\mathbf{s}_2, \mathbf{a}')$$

Overestimation

$$y_i = r_i + \gamma \max_{\mathbf{a}'} Q^k(\mathbf{s}', \mathbf{a}')$$

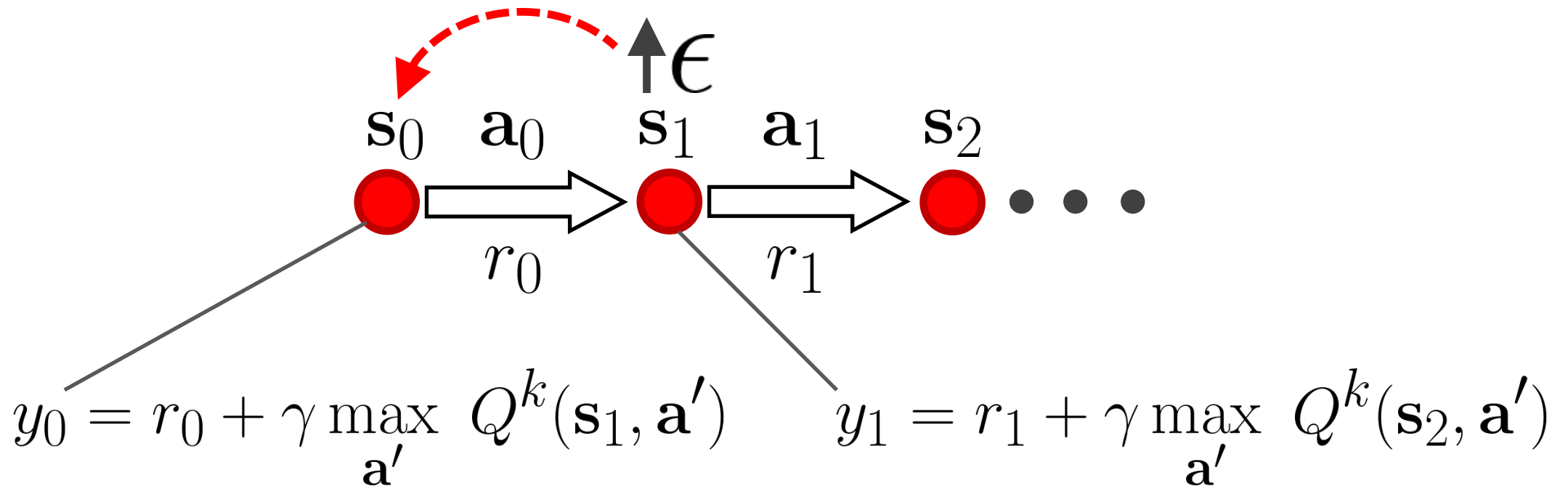
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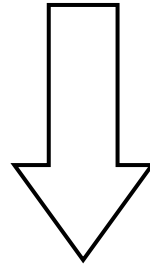
Overestimation

$$y_i = r_i + \gamma \max_{\mathbf{a}'} \underline{Q^k(\mathbf{s}', \mathbf{a}')}$$

Target network can slow
propagation of errors

Overestimation

$$y_i = r_i + \gamma \max_{\mathbf{a}'} Q^k(\mathbf{s}', \mathbf{a}')$$



$$y_i = r_i + \gamma \underbrace{Q^k}_{\text{action evaluation}} \left(\mathbf{s}', \underbrace{\arg \max_{\mathbf{a}'} Q^k(\mathbf{s}', \mathbf{a}')}_{\text{action selection}} \right)$$

action evaluation

action selection

Double Q-Learning

Decouple selection from evaluation by using *different* Q-functions

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Double Q-Learning

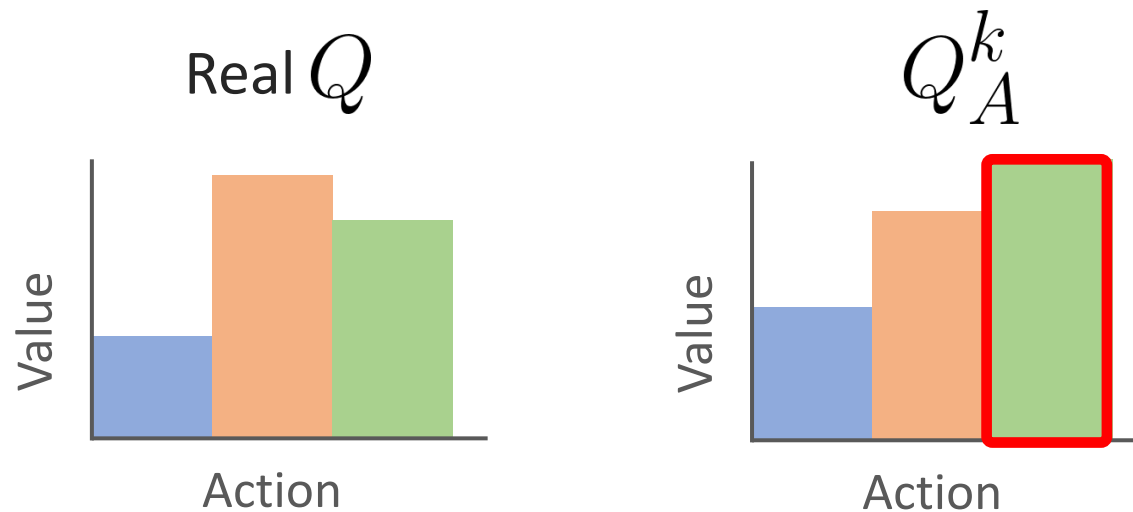
Decouple selection from evaluation by using *different* Q-functions

$$y_i = r_i + \gamma \underbrace{Q_B^k}_{\text{action evaluation}} \left(\mathbf{s}', \arg \max_{\mathbf{a}'} \underbrace{Q_A^k(\mathbf{s}', \mathbf{a}')}_{\text{action selection}} \right)$$

Double Q-Learning

Decouple selection from evaluation by using *different* Q-functions

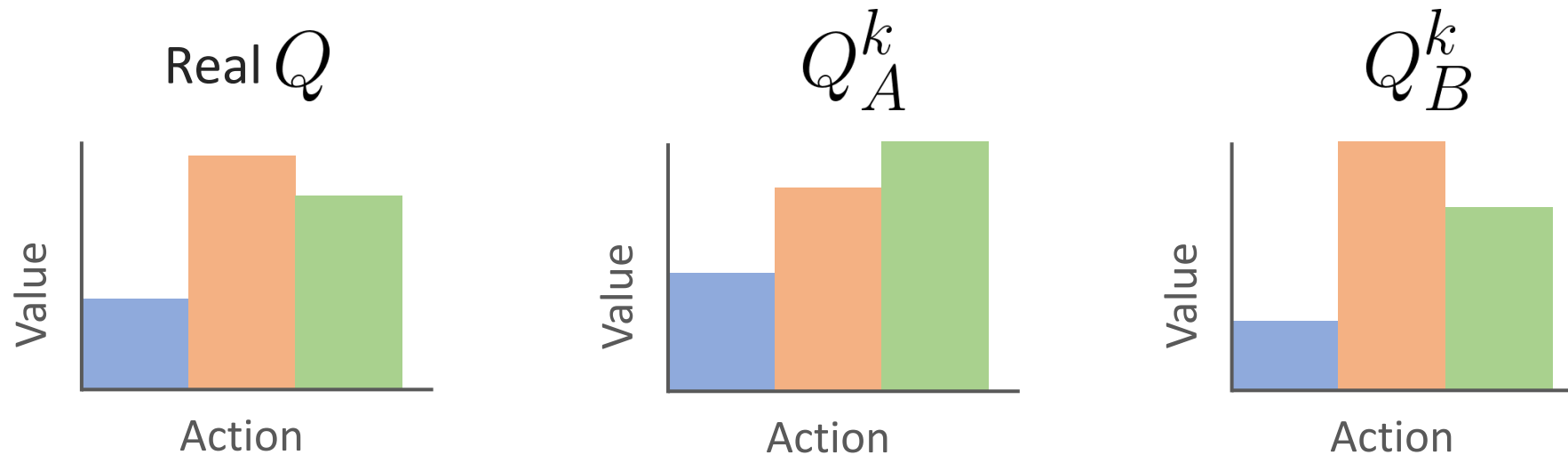
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Decouple selection from evaluation by using *different* Q-functions

$$y_i = r_i + \gamma Q_B^k \left(\mathbf{s}', \arg \max_{\mathbf{a}'} Q_A^k(\mathbf{s}', \mathbf{a}') \right)$$

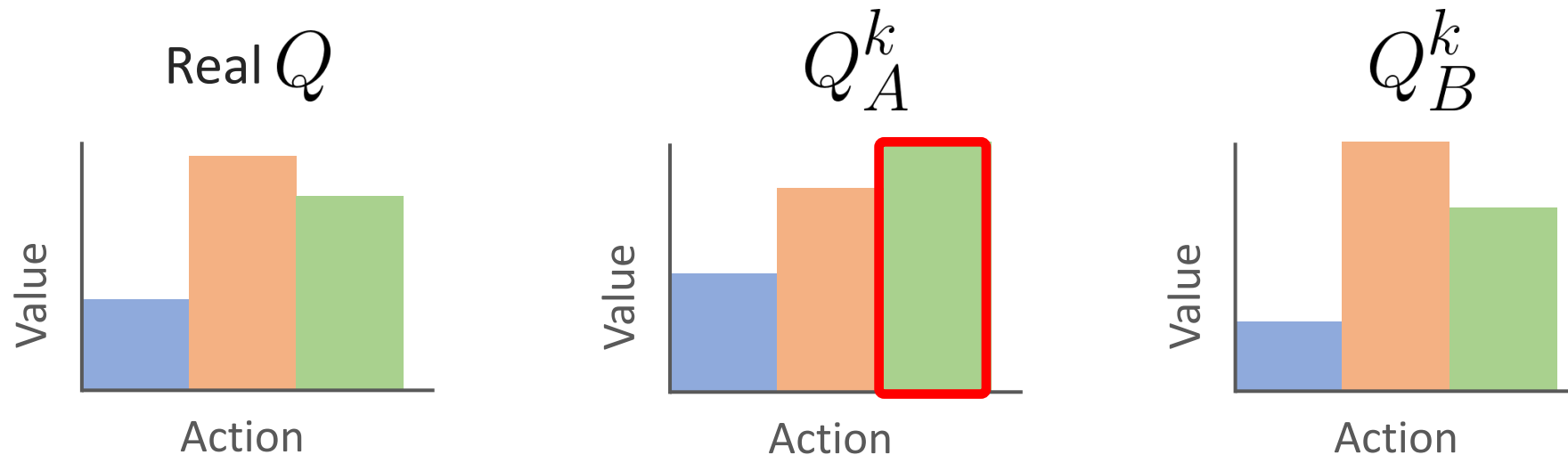


Double Q-Learning

Decouple selection from evaluation by using *different* Q-functions

$$y_i = r_i + \gamma Q_B^k \left(s', \arg \max_{a'} Q_A^k(s', a') \right)$$

action selection

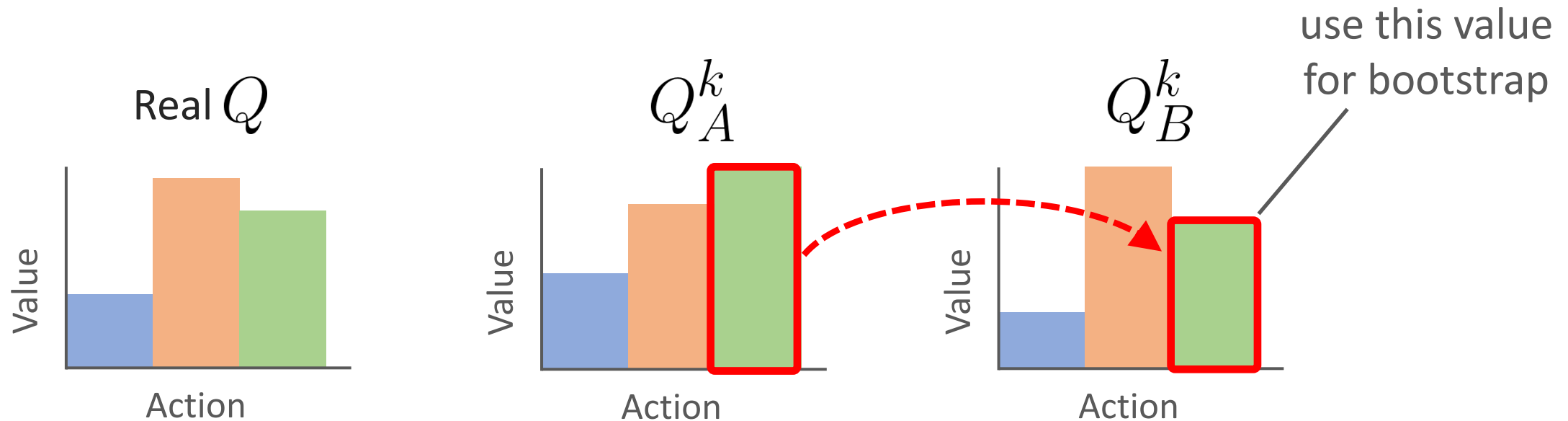


Double Q-Learning

Decouple selection from evaluation by using *different* Q-functions

$$y_i = r_i + \gamma \underbrace{Q_B^k}_{\text{action evaluation}} \left(\mathbf{s}', \arg \max_{\mathbf{a}'} Q_A^k(\mathbf{s}', \mathbf{a}') \right)$$

action evaluation



Implementation

Option 1: Train two separate Q-functions

$$y_i = r_i + \gamma Q_B^k \left(\mathbf{s}', \arg \max_{\mathbf{a}'} Q_A^k(\mathbf{s}', \mathbf{a}') \right)$$

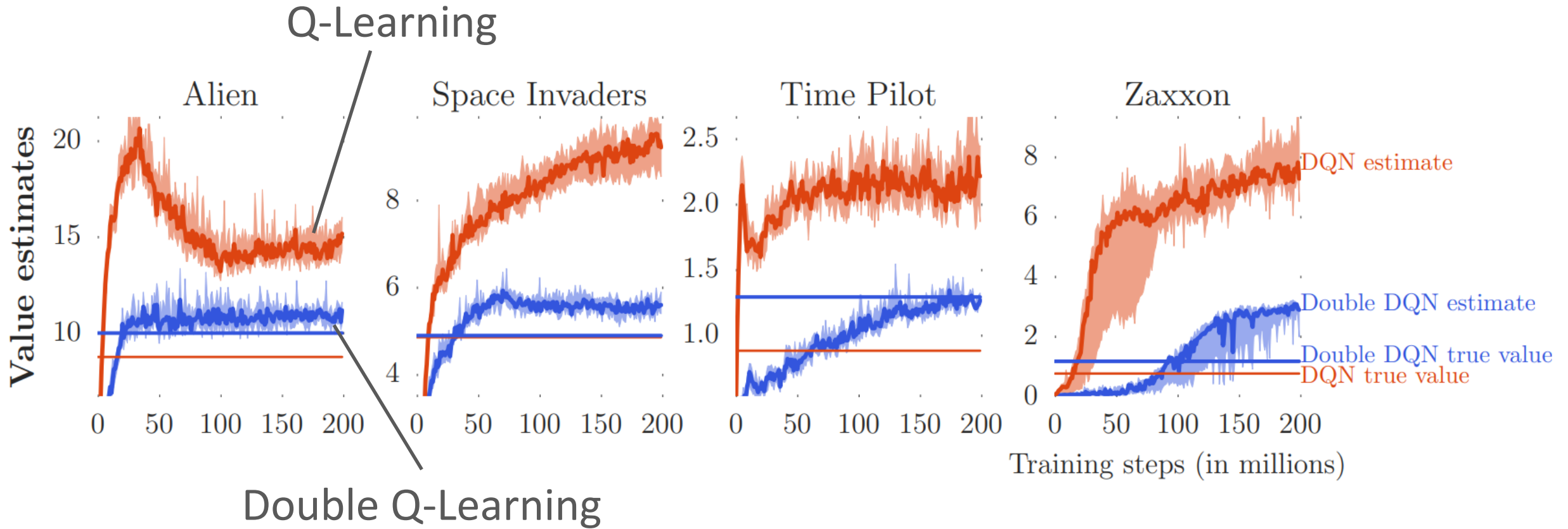
Option 2: Use target network

$$y_i = r_i + \gamma \underline{Q'} \left(\mathbf{s}', \arg \max_{\mathbf{a}'} \underline{Q^k}(\mathbf{s}', \mathbf{a}') \right)$$

target network

main Q-network

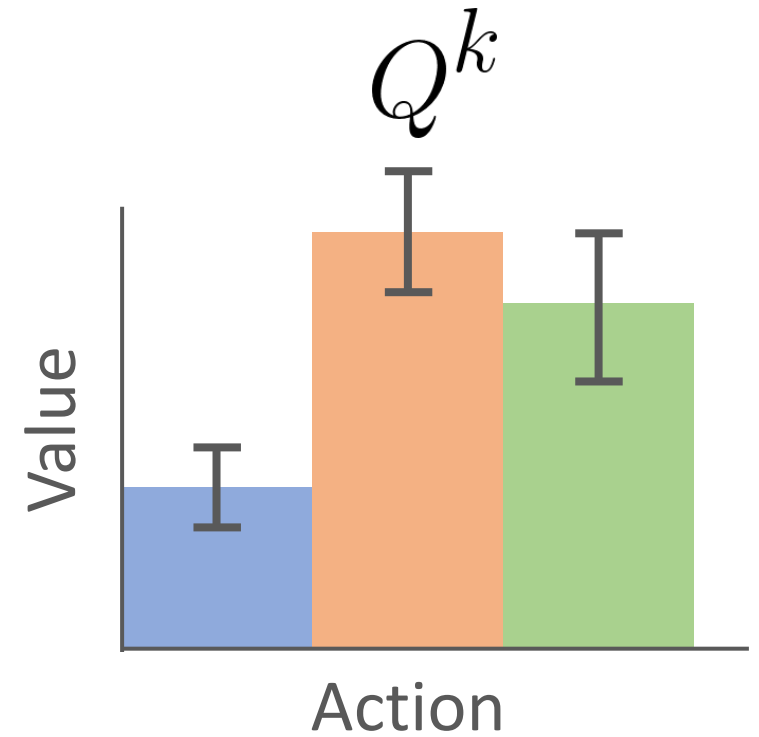
Double Q-Learning



Deep Reinforcement Learning with Double Q-learning
[van Hasselt et al. 2016]

Pessimistic Estimate

- Source of overestimation is model error
- Can we estimate model uncertainty for Q-function?



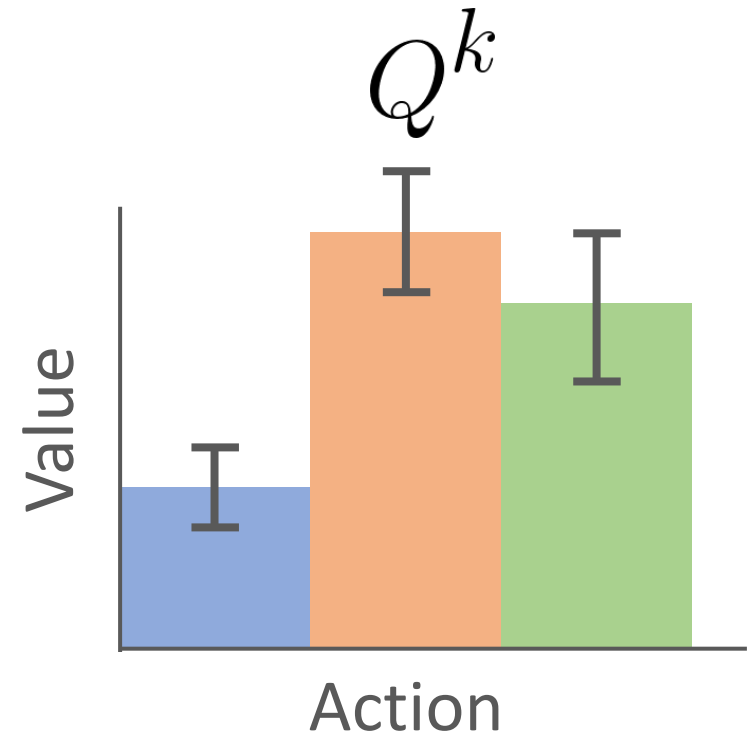
Pessimistic Estimate

- Source of overestimation is model error
- Can we estimate model uncertainty for Q-function?

Error: $[-\epsilon, \epsilon]$

$$y_i = r_i + \gamma \left(\max_{\mathbf{a}'} Q^k(\mathbf{s}', \mathbf{a}') - \epsilon \right)$$

lower bound



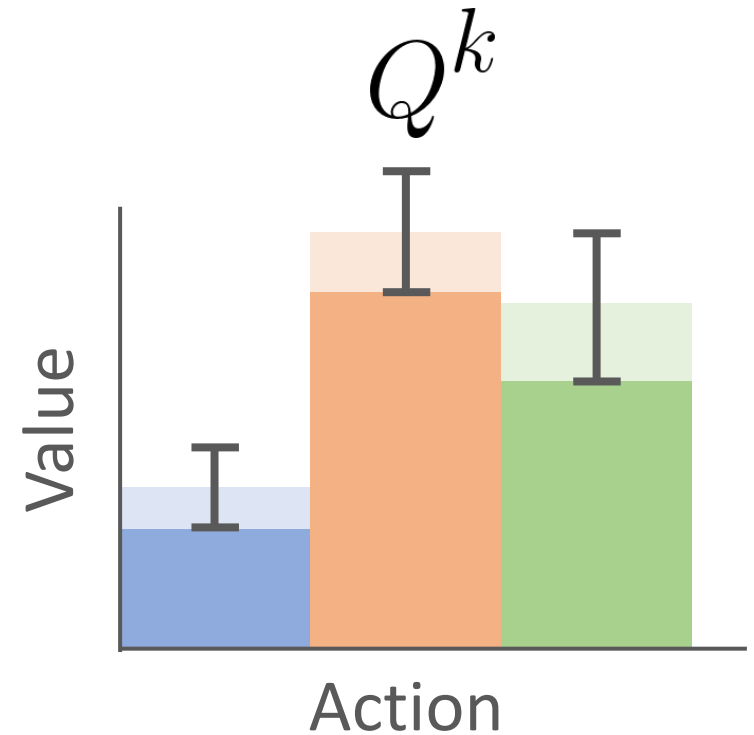
Pessimistic Estimate

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Error: $[-\epsilon, \epsilon]$

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lower bound



Ensemble

- Estimate model uncertainty with an ensemble $\{Q_1, Q_2, \dots\}$

$$y_i = r_i + \gamma \max_{\mathbf{a}'} \min_j Q_j(\mathbf{s}', \mathbf{a}')$$

pessimistic value estimate

REDQ

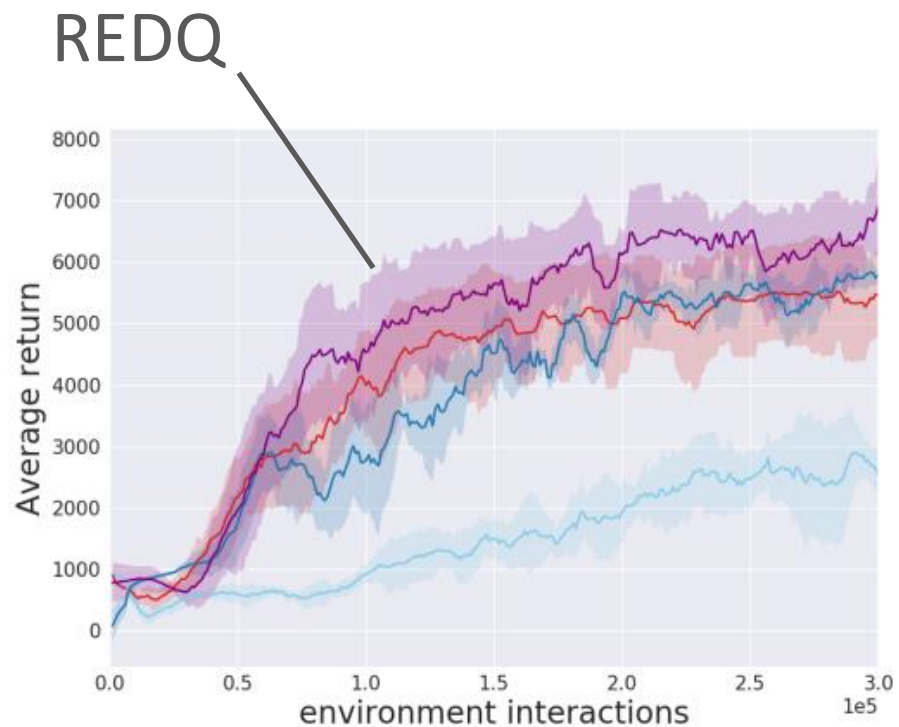
- Compute minimum over a random subset of the ensemble

$$\mathcal{M} \subseteq \{Q_1, Q_2, \dots\}$$

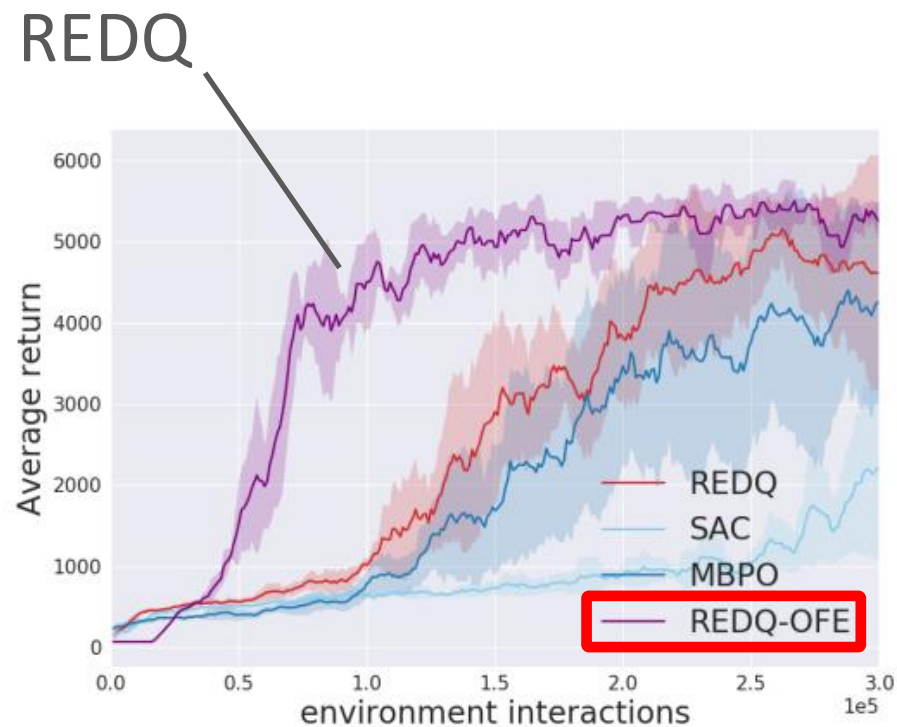
$$y_i = r_i + \gamma \max_{\mathbf{a}'} \min_{j \in \mathcal{M}} Q_j(\mathbf{s}', \mathbf{a}')$$

- in practice, randomly sampling 2 Q-functions work well

REDQ



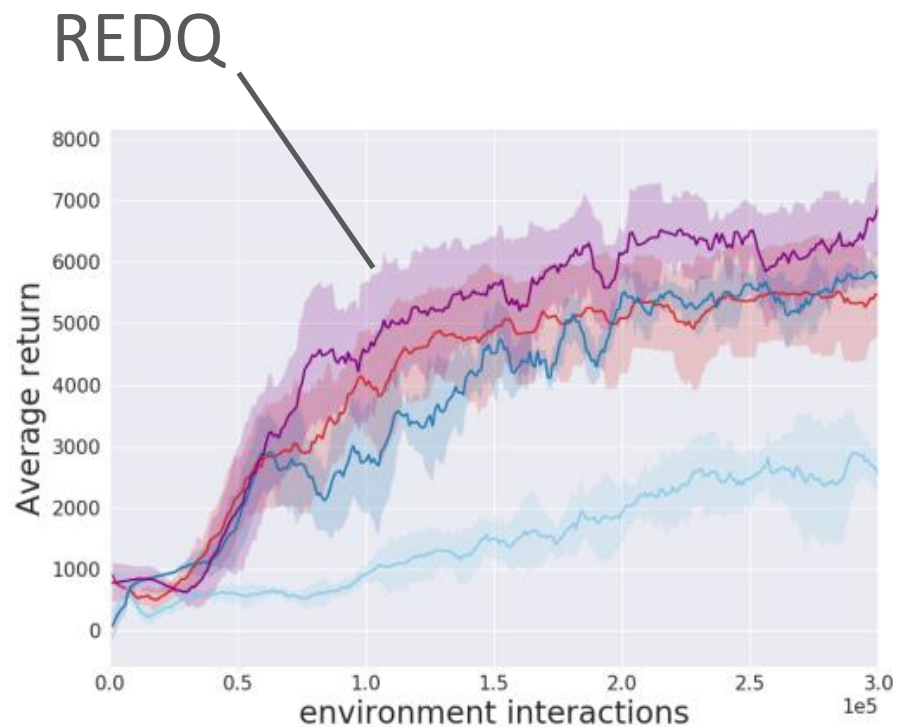
(a) Performance, Ant



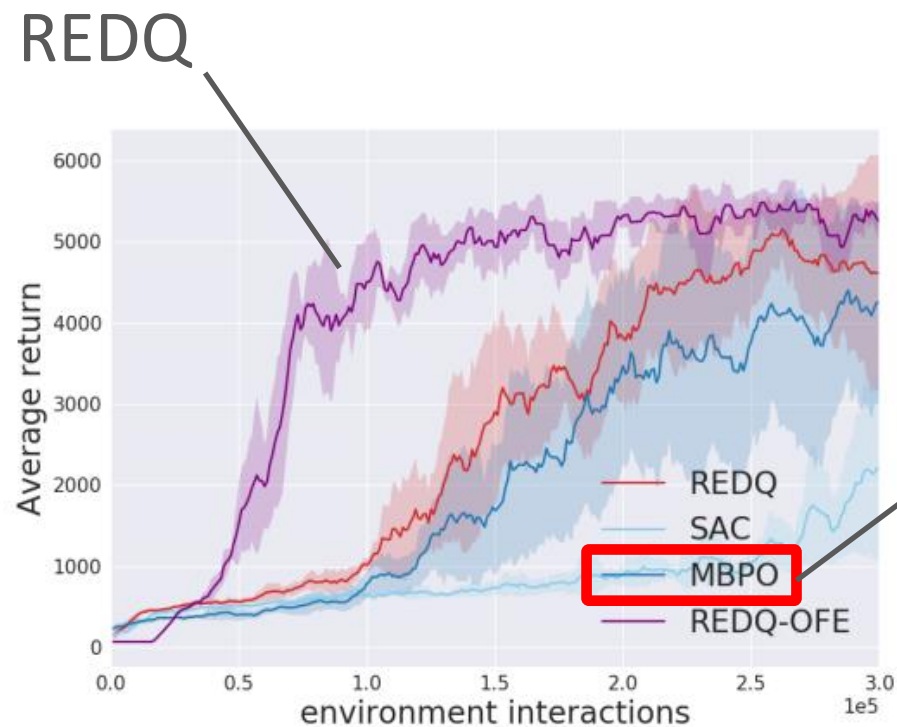
(b) Performance, Humanoid

Randomized Ensembled Double Q-Learning: Learning Fast Without a Model
[Chen et al. 2021]

REDQ



(a) Performance, Ant



(b) Performance, Humanoid

Model-Based RL

Randomized Ensembled Double Q-Learning: Learning Fast Without a Model

[Chen et al. 2021]

REDQ

- Compute minimum over a random subset of the ensemble $\mathcal{M} \subseteq \{Q_1, Q_2, \dots\}$

$$y_i = r_i + \gamma \max_{\mathbf{a}'} \min_{j \in \mathcal{M}} Q_j(\mathbf{s}', \mathbf{a}')$$

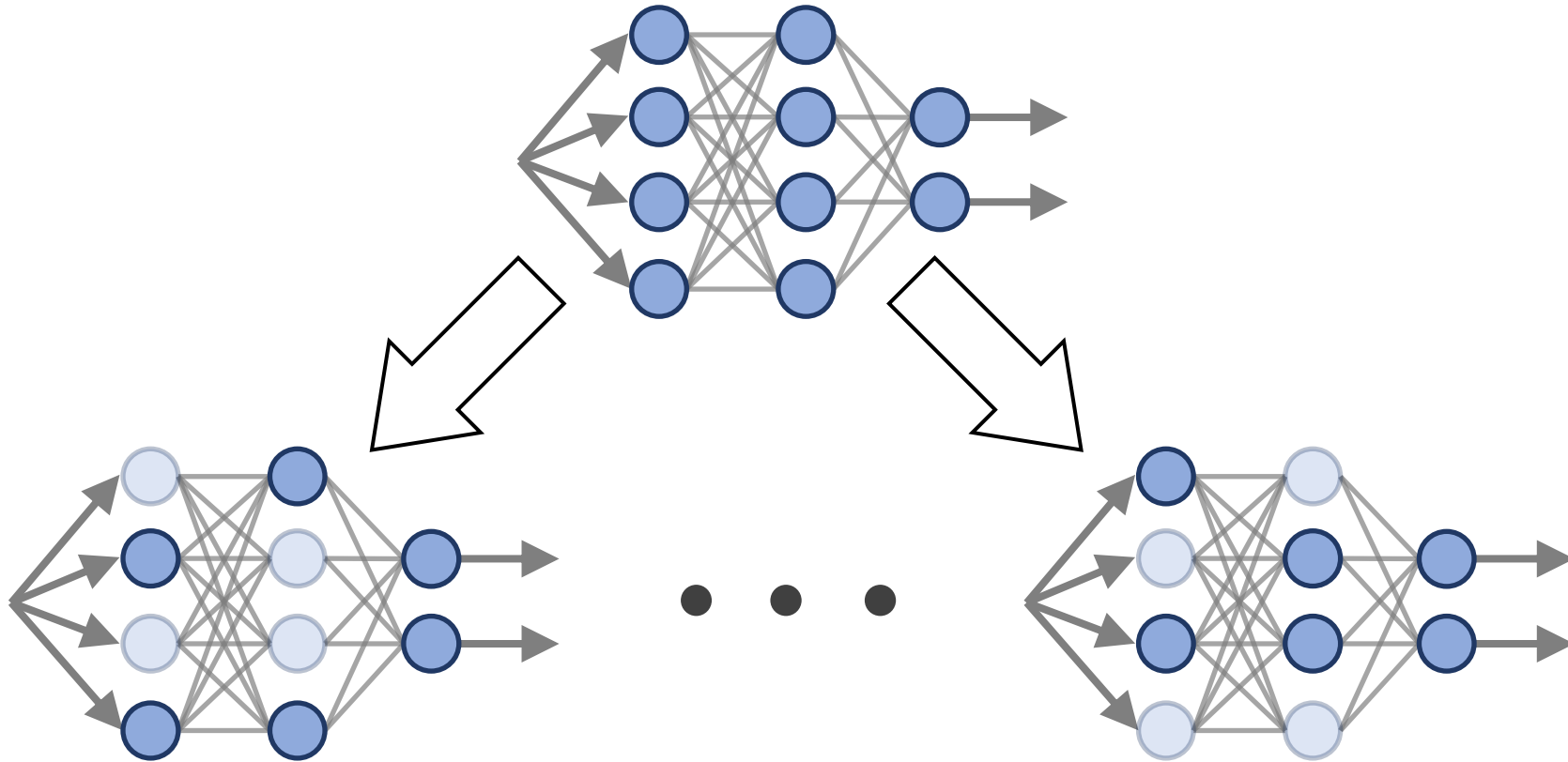
- in practice, randomly sampling 2 Q-functions work well

Drawback:

- Need to train multiple Q-functions

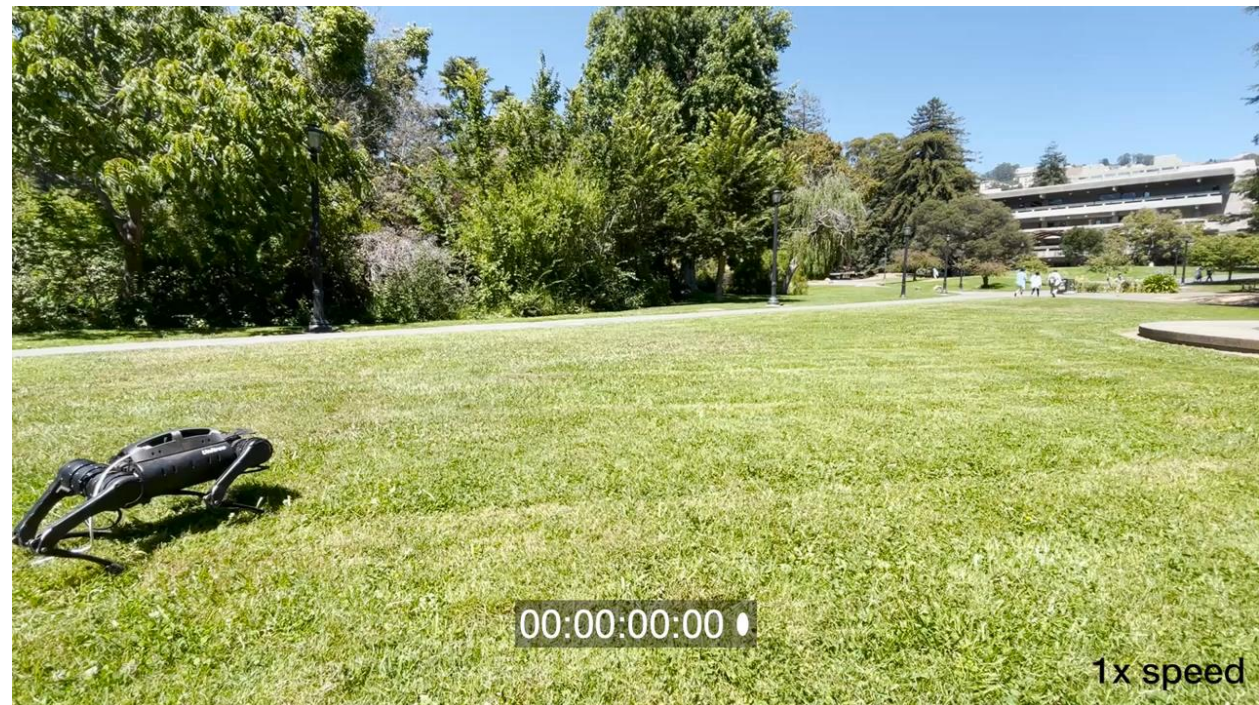
DroQ

- Instead of training an ensemble, emulate an ensemble using Dropout



Dropout Q-Functions for Doubly Efficient Reinforcement Learning
[Hiraoka et al. 2022]

DroQ

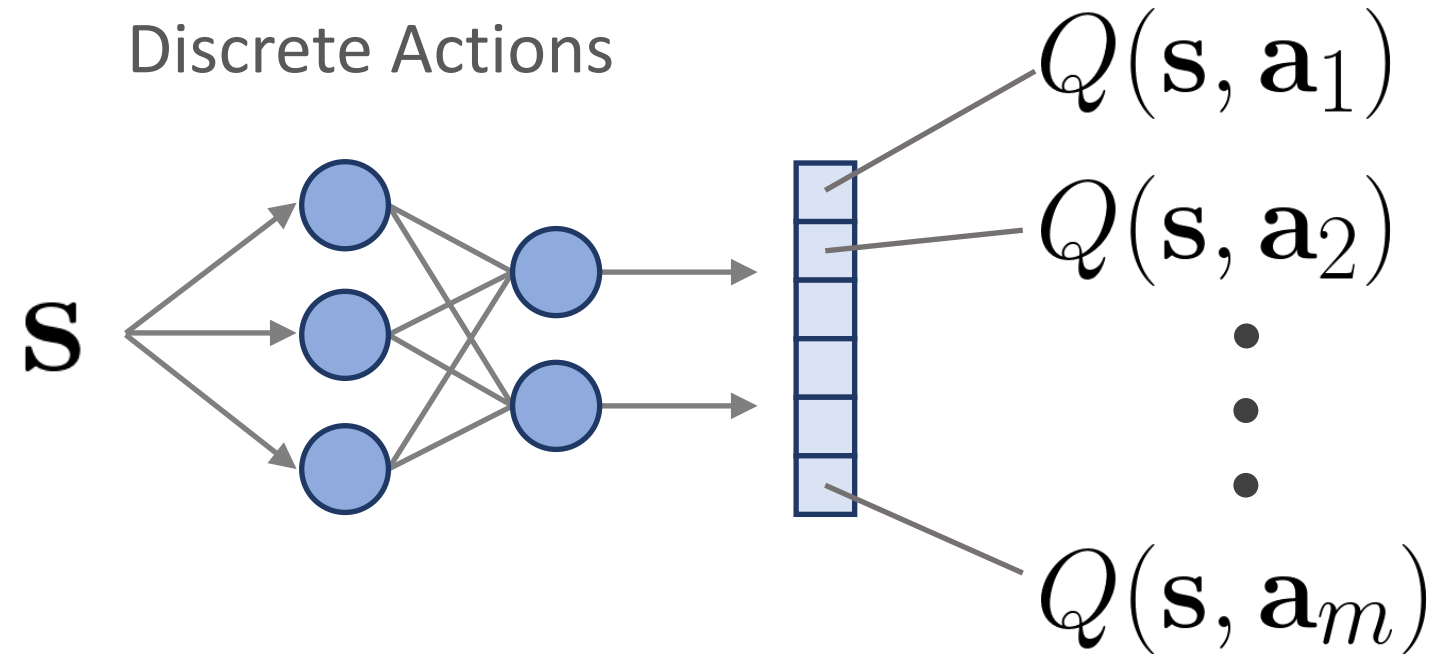


A Walk in the Park: Learning to Walk in 20 Minutes With Model-Free Reinforcement Learning
[Smith et al. 2022]

Overview

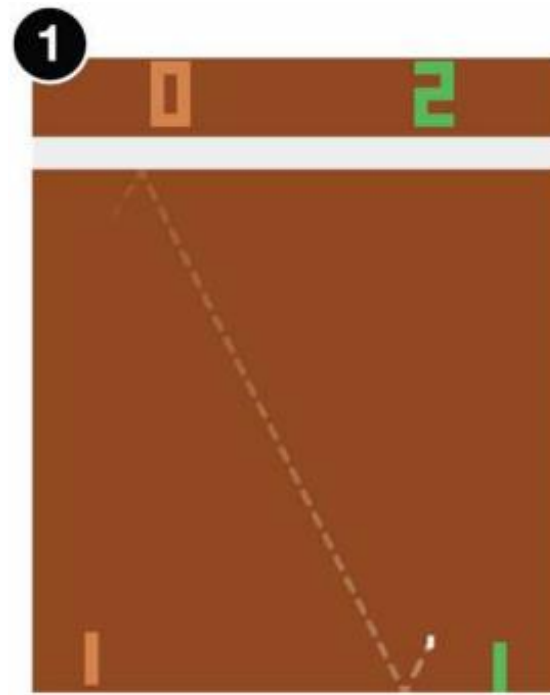
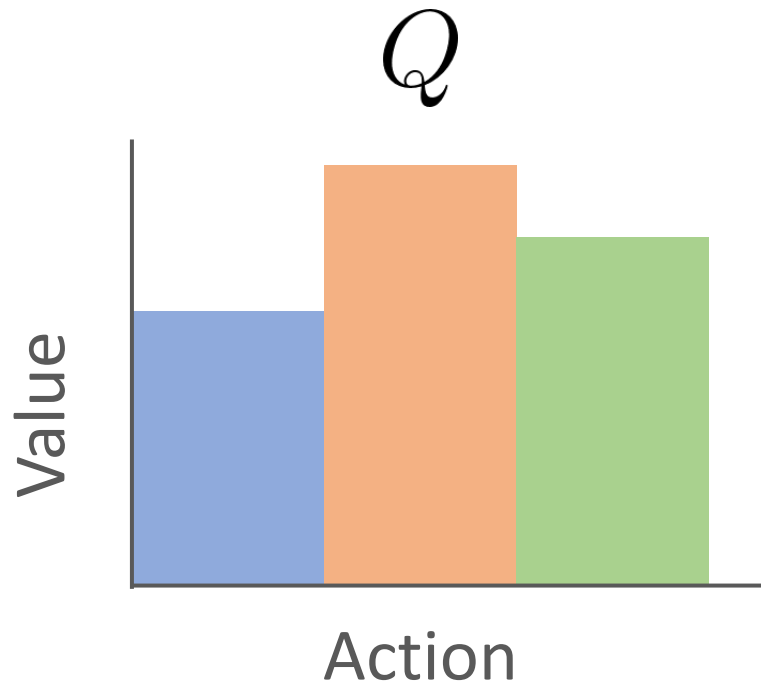
- Nonstationary Targets → Target Networks
- Overestimation → Pessimistic Estimates
- **Model Architecture**

Model Architecture



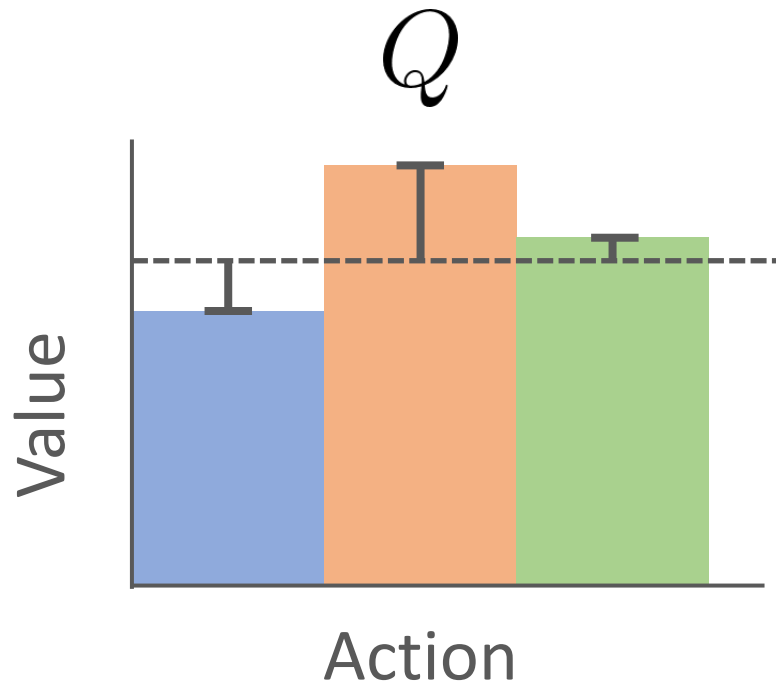
Model Architecture

- Q-values at a particular state often do not vary that much



Model Architecture

- Q-values at a particular state often do not vary that much
- Only the *relative* values are needed to select actions



Model Architecture

$$A^\pi(\mathbf{s}, \mathbf{a}) = Q^\pi(\mathbf{s}, \mathbf{a}) - \underline{V^\pi(\mathbf{s})}$$



Model Architecture

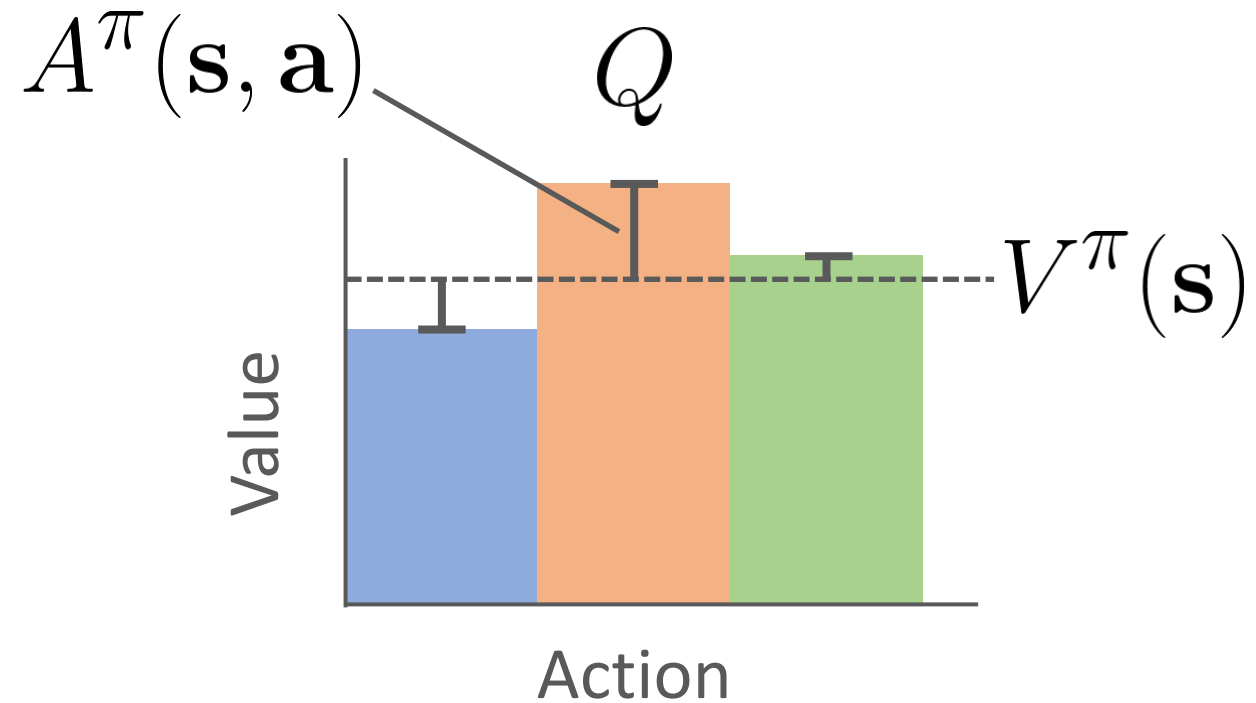
$$Q^\pi(\mathbf{s}, \mathbf{a}) = \underbrace{V^\pi(\mathbf{s})}_{\text{Action-independent value function}} + \underbrace{A^\pi(\mathbf{s}, \mathbf{a})}_{\text{Action-dependent advantage function}}$$

Action-independent
value function

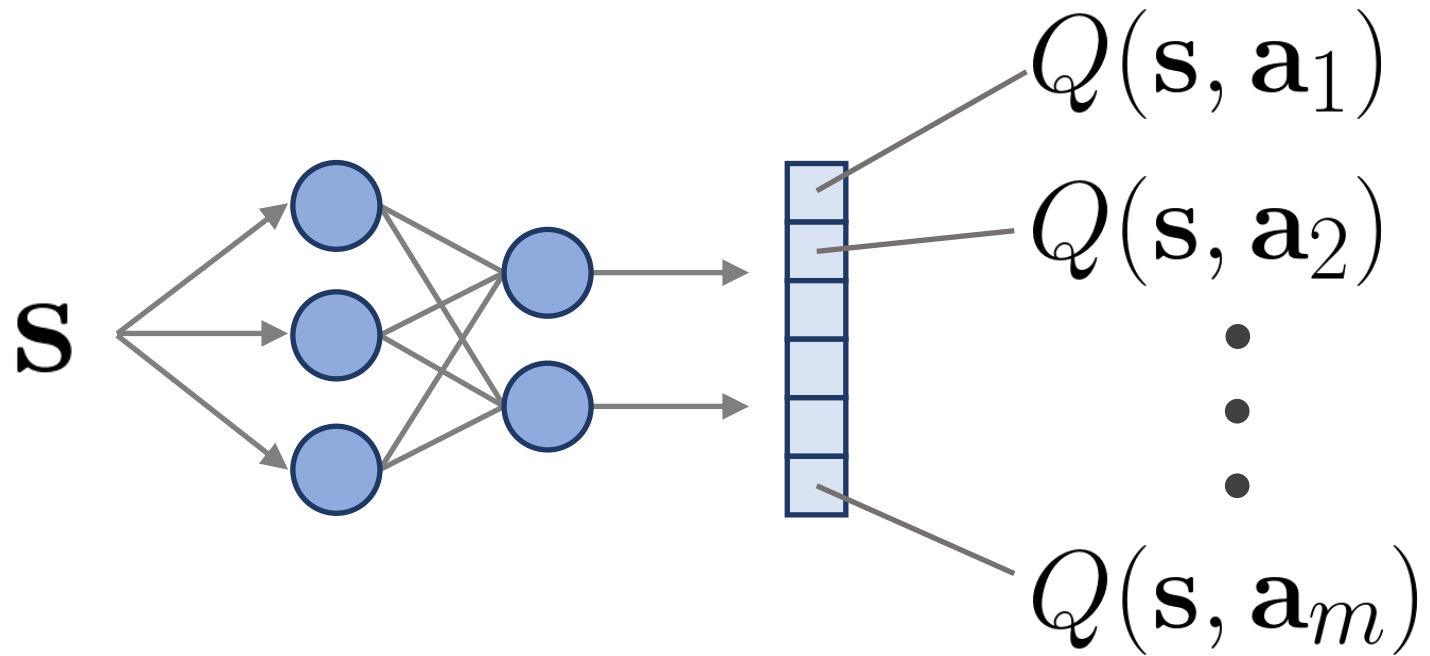
Action-dependent
advantage function

Model Architecture

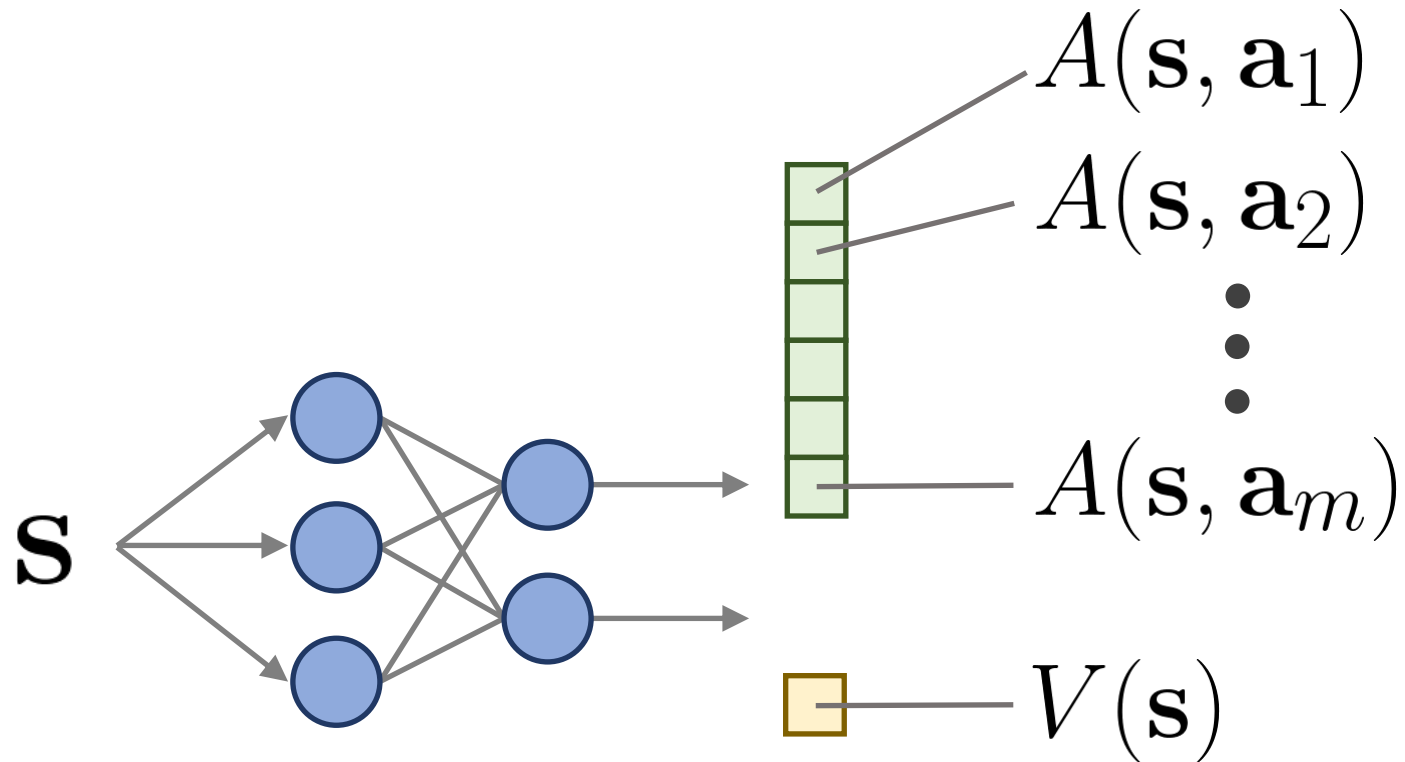
$$Q^\pi(\mathbf{s}, \mathbf{a}) = \underline{V^\pi(\mathbf{s})} + \underline{A^\pi(\mathbf{s}, \mathbf{a})}$$



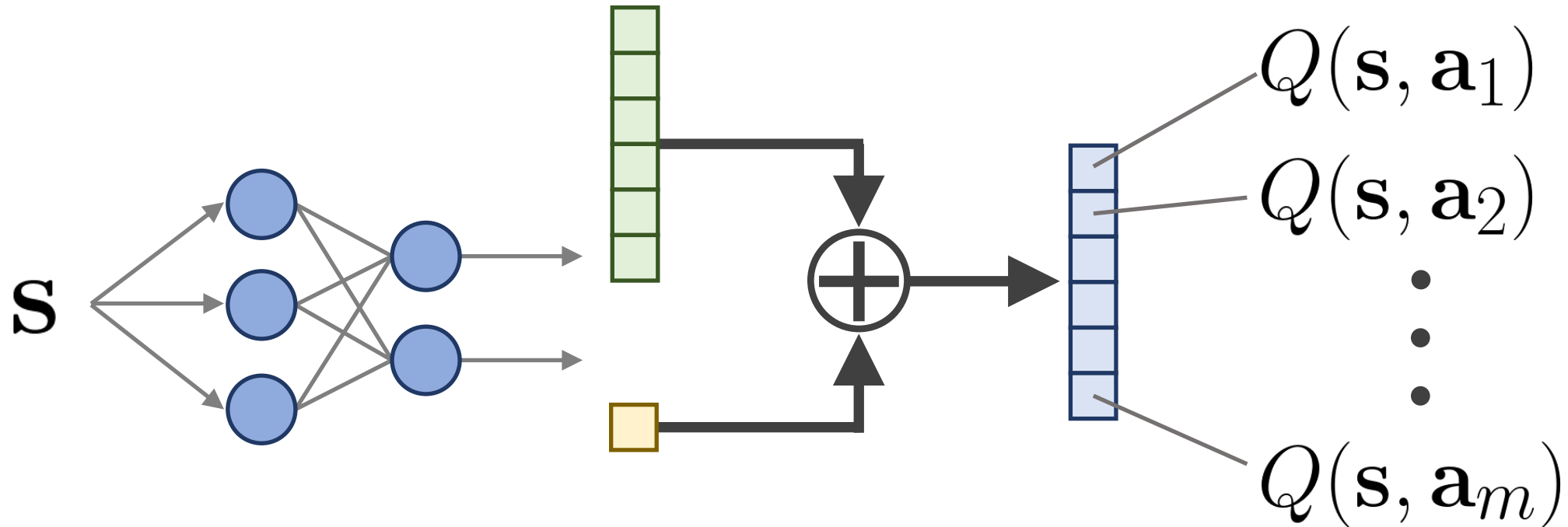
Dueling Q-Networks



Dueling Q-Networks

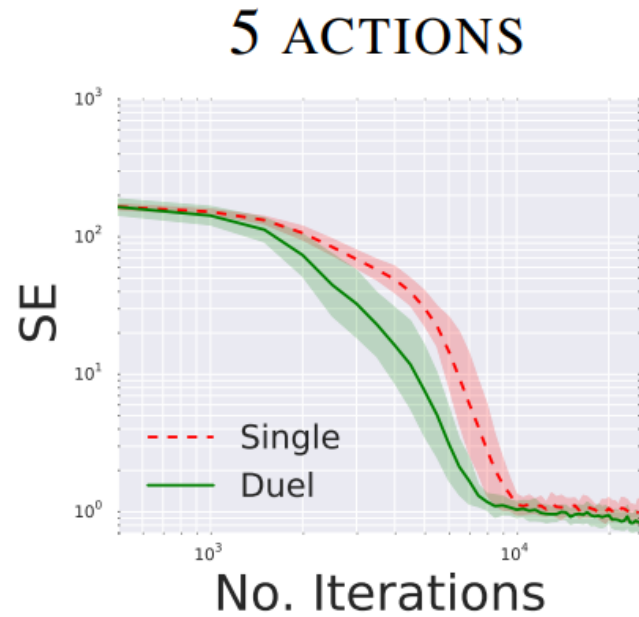


Dueling Q-Networks

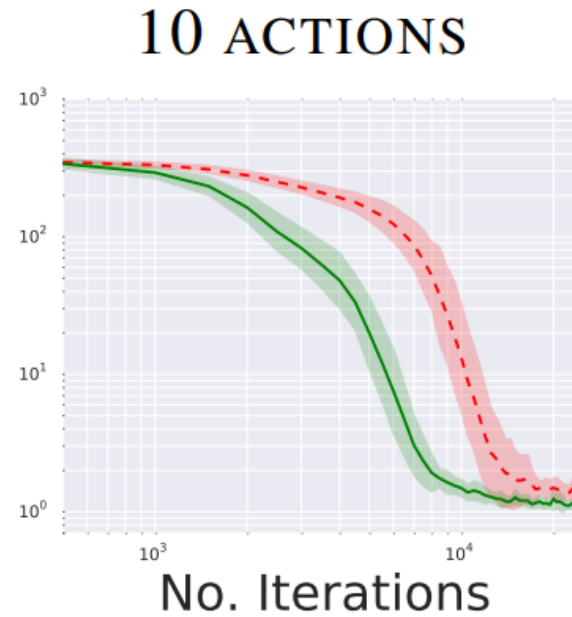


Dueling Network Architectures for Deep Reinforcement Learning
[Wang et al. 2016]

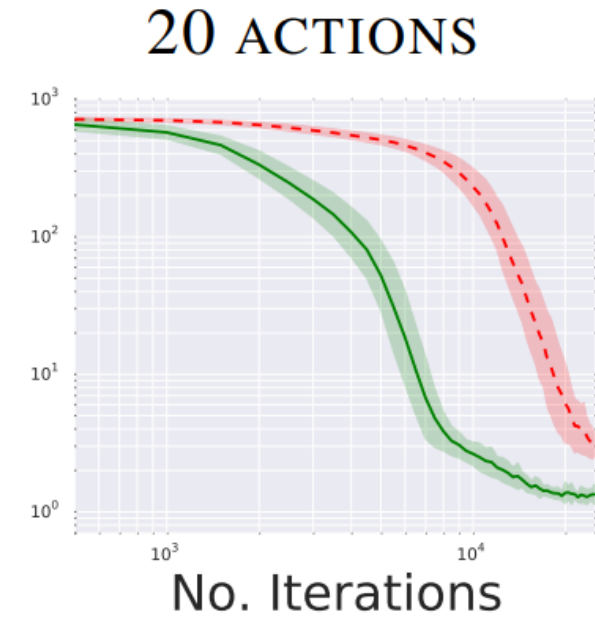
Dueling Q-Networks



(b)



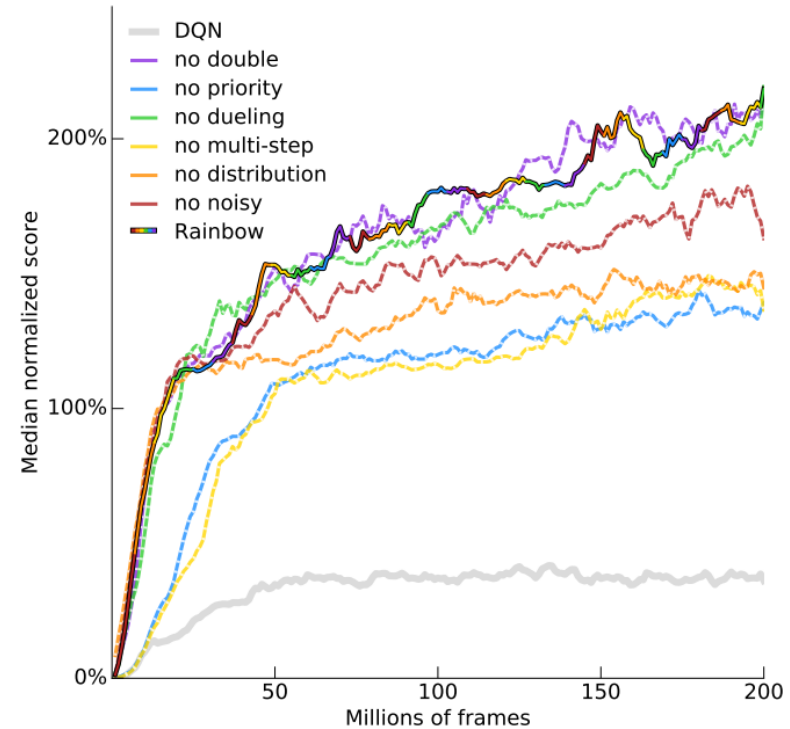
(c)



(d)

Lots of Tricks

- Prioritized Replay
- Multi-Step Returns
- Distributional RL
- Noisy Nets
- Etc...



Note: techniques for improving Q-Learning can also be applied to other algorithms (e.g. DDPG, SAC, TD3, MPO, etc.)

Summary

- Target Networks
- Overestimation
- Model Architecture