Model-Based Reinforcement Learning

CMPT 729 G100

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Overview

- Model-Based RL
- DYNA
- Model Representations
- Uncertainty Estimation
- MPC

Taxonomy of RL Algorithms

- Policy-Based Methods
- Value-Based Methods
- Actor-Critic Methods
- Model-Based Methods



Sample Complexity



Simulation

Learning Agile Robotic Locomotion Skills by Imitating Animals [Peng et al. 2020]

Sample Complexity



Simulation

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Sample Complexity



Simulation

Real World

Learning Agile Robotic Locomotion Skills by Imitating Animals [Peng et al. 2020]

Sim-to-Real



Simulation (Low-Fidelity) Building a good simulator is hard

Can we learn a simulator?



Simulation (High-Fidelity) **Real World**

Reinforcement Learning for Robust Parameterized Locomotion Control of Bipedal Robots [Li et al. 2021]

Dynamics Model



Why Learn a Dynamics Model?



Simple Dynamics

Complex Dynamics

Dynamics Model

• Learn a dynamics model:



Learning Dynamics Model

- Collect data with a base policy π_0

$$\mathbf{s}_{0} \quad \mathbf{a}_{0} \quad \mathbf{s}_{1} \quad \mathbf{a}_{1} \quad \mathbf{s}_{2} \quad \mathbf{s}_{T-1} \quad \mathbf{a}_{T-1} \mathbf{s}_{T}$$

- Dataset: $\mathcal{D} = \{(\mathbf{s}_i, \mathbf{a}_i, \mathbf{s}'_i)\}$
- Fit a dynamics model via supervised learning

$$\underset{f}{\arg \max} \mathbb{E}_{(\mathbf{s},\mathbf{a},\mathbf{s'})\sim\mathcal{D}} \left[\log f(\mathbf{s'}|\mathbf{s},\mathbf{a})\right]$$

Model-Based RL

- Collect data with a base policy π_0

$$\mathbf{s}_{0} \quad \mathbf{a}_{0} \quad \mathbf{s}_{1} \quad \mathbf{a}_{1} \quad \mathbf{s}_{2} \quad \mathbf{s}_{T-1} \quad \mathbf{a}_{T-1} \quad \mathbf{s}_{T}$$

• Dataset:
$$\mathcal{D} = \{(\mathbf{s}_i, \mathbf{a}_i, \mathbf{s}_i')\}$$

• Fit a dynamics model via supervised learning

$$\underset{f}{\arg \max} \mathbb{E}_{(\mathbf{s},\mathbf{a},\mathbf{s'})\sim\mathcal{D}} \left[\log f(\mathbf{s'}|\mathbf{s},\mathbf{a})\right]$$

- Train new policy π by simulating with $f(\mathbf{s'}|\mathbf{s},\mathbf{a})$

















Distribution Shift

• Data distribution is different from the policy's distribution

$$\mathcal{D} \sim p(\mathbf{s}, \mathbf{a} | \pi_0) \neq p(\mathbf{s}, \mathbf{a} | \pi)$$

- Model $f(\mathbf{s'}|\mathbf{s}, \mathbf{a})$ trained on \mathcal{D} Low error under $p(\mathbf{s}, \mathbf{a}|\pi_0)$

 - High error under $p(\mathbf{s},\mathbf{a}|\pi)$
- Can we make

$$p(\mathbf{s}, \mathbf{a} | \pi_0) = p(\mathbf{s}, \mathbf{a} | \pi)?$$



Model-Based RL

• Collect data with a base policy π_0

$$\mathbf{s}_{0} \quad \mathbf{a}_{0} \quad \mathbf{s}_{1} \quad \mathbf{a}_{1} \quad \mathbf{s}_{2} \quad \mathbf{s}_{T-1} \quad \mathbf{a}_{T-1} \quad \mathbf{s}_{T}$$

• Dataset:
$$\mathcal{D} = \{(\mathbf{s}_i, \mathbf{a}_i, \mathbf{s}_i')\}$$

• Fit a dynamics model via supervised learning

$$\underset{f}{\operatorname{arg max}} \mathbb{E}_{(\mathbf{s},\mathbf{a},\mathbf{s'})\sim\mathcal{D}} \left[\log f(\mathbf{s'}|\mathbf{s},\mathbf{a})\right]$$

• Train new policy π by simulating with f

ALGORITHM: DYNA

- 1: $\pi^0 \leftarrow \text{initialize policy}$
- 2: $\mathcal{D} \leftarrow \{\emptyset\}$ initialize dataset
- 3: for iteration k = 0, ..., n 1 do
- 4: Sample trajectory τ according to $\pi^k(\mathbf{a}|\mathbf{s})$
- 5: Add transitions to dataset $\mathcal{D} = \mathcal{D} \cup \{(\mathbf{s}_i, \mathbf{a}_i, \mathbf{s}'_i)\}$
- 6: Fit dynamics model: $f = \arg \max_{f} \mathbb{E}_{(\mathbf{s}, \mathbf{a}, \mathbf{s}') \sim \mathcal{D}} \left[\log f(\mathbf{s}' | \mathbf{s}, \mathbf{a}) \right]$

7: $\pi^{k+1} \leftarrow$ train policy by simulating rollouts with $f(\mathbf{s'}|\mathbf{s}, \mathbf{a})$ 8: end for

9: return π^n

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ALGORITHM: DYNA

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- 2: $\mathcal{D} \leftarrow \{\emptyset\}$ initialize dataset

3: for iteration k = 0, ..., n - 1 do

- 4: Sample trajectory τ according to $\pi^k(\mathbf{a}|\mathbf{s})$
- 5: Add transitions to dataset $\mathcal{D} = \mathcal{D} \cup \{(\mathbf{s}_i, \mathbf{a}_i, \mathbf{s}'_i)\}$
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 $f = \arg \max_{f} \mathbb{E}_{(\mathbf{s}, \mathbf{a}, \mathbf{s}') \sim \mathcal{D}} [\log f(\mathbf{s}' | \mathbf{s}, \mathbf{a})]$



ALGORITHM: DYNA

- 1: $\pi^0 \leftarrow \text{initialize policy}$
- 2: $\mathcal{D} \leftarrow \{\emptyset\}$ initialize dataset

3: for iteration
$$k = 0, ..., n - 1$$
 do
4: Sample trajectory τ according to $\pi^k(\mathbf{a}|\mathbf{s})$ all iterations
5: Add transitions to dataset $\mathcal{D} = \mathcal{D} \cup \{(\mathbf{s}_i, \mathbf{a}_i, \mathbf{s}'_i)\}$

6: Fit dynamics model:

$$f = \arg \max_{f} \mathbb{E}_{(\mathbf{s}, \mathbf{a}, \mathbf{s}') \sim \mathcal{D}} [\log f(\mathbf{s}' | \mathbf{s}, \mathbf{a})]$$

7: $\pi^{k+1} \leftarrow \text{train policy by simulating rollouts with } f(\mathbf{s}'|\mathbf{s}, \mathbf{a})$ 8: end for

9: return π^n

Model Representation

- How do we represent $f(\mathbf{s'}|\mathbf{s},\mathbf{a})$?
- MDP with small discrete states and actions → lookup table



Deterministic Models

• How do we represent $f(\mathbf{s'}|\mathbf{s},\mathbf{a})$?

$$\underset{f}{\arg\min} \mathbb{E}_{(\mathbf{s},\mathbf{a},\mathbf{s}')\sim\mathcal{D}} \left[\left| \left| \mathbf{s}' - f(\mathbf{s},\mathbf{a}) \right| \right|^2 \right]$$

What if the dynamics are stochastic?



Stochastic Models

- How do we represent $f(\mathbf{s'}|\mathbf{s},\mathbf{a})$?

$$\underset{f}{\operatorname{arg max}} \mathbb{E}_{(\mathbf{s},\mathbf{a},\mathbf{s'})\sim\mathcal{D}} \left[\log f(\mathbf{s'}|\mathbf{s},\mathbf{a})\right]$$


Stochastic Models

• How do we represent $f(\mathbf{s'}|\mathbf{s},\mathbf{a})$?

$$\underset{f}{\operatorname{arg max}} \mathbb{E}_{(\mathbf{s},\mathbf{a},\mathbf{s'})\sim\mathcal{D}} \left[\log f(\mathbf{s'}|\mathbf{s},\mathbf{a}) \right]$$

Conditional Generative Model

- Variational Autoencoders (VAEs)
- Generative Adversarial Networks (GANs)
- Flow Models
- Diffusion Models
- Etc.

Reward Model

- If reward function is unknown, augment model to predict both states and rewards
- For most tasks, reward function is available/specified by a human

dynamics model $f(\mathbf{s'}|\mathbf{s},\mathbf{a})$

reward model

$$h(r|\mathbf{s}, \mathbf{a}, \mathbf{s'})$$

Model-Based Rollout

ALGORITHM: DYNA

- 1: $\pi^0 \leftarrow \text{initialize policy}$
- 2: $\mathcal{D} \leftarrow \{\emptyset\}$ initialize dataset
- 3: for iteration k = 0, ..., n 1 do
- 4: Sample trajectory τ according to $\pi^k(\mathbf{a}|\mathbf{s})$
- 5: Add transitions to dataset $\mathcal{D} = \mathcal{D} \cup \{(\mathbf{s}_i, \mathbf{a}_i, \mathbf{s}'_i)\}$
- 6: Fit dynamics model:

 $f = \arg \max_{f} \mathbb{E}_{(\mathbf{s}, \mathbf{a}, \mathbf{s}') \sim \mathcal{D}} [\log f(\mathbf{s}' | \mathbf{s}, \mathbf{a})]$



Dyna, an Integrated Architecture for Learning, Planning, and Reacting [Sutton 1991]

Model-Based Rollout



Drift

- Same action sequence in the real env and the model can lead to very different trajectories
- Autoregressive model \rightarrow compounding error



Drift



Model-Based Rollout







Model-Based RL



(a) Example task domains.

(b) NAF and DDPG on multi-target reacher.

(c) NAF and DDPG on peg insertion.

Continuous Deep Q-Learning with Model-based Acceleration [Gu et al. 2016]

DYNA

ALGORITHM: DYNA

- 1: $\pi^0 \leftarrow \text{initialize policy}$
- 2: $\mathcal{D} \leftarrow \{\emptyset\}$ initialize dataset
- 3: for iteration k = 0, ..., n 1 do
- 4: Sample trajectory τ according to $\pi^k(\mathbf{a}|\mathbf{s})$
- 5: Add transitions to dataset $\mathcal{D} = \mathcal{D} \cup \{(\mathbf{s}_i, \mathbf{a}_i, \mathbf{s}'_i)\}$
- 6: Fit dynamics model:

 $f = \arg \max_{f} \mathbb{E}_{(\mathbf{s}, \mathbf{a}, \mathbf{s}') \sim \mathcal{D}} [\log f(\mathbf{s}' | \mathbf{s}, \mathbf{a})]$



Dyna, an Integrated Architecture for Learning, Planning, and Reacting [Sutton 1991]



(e.g. policy gradient, Q-learning, SAC, etc.)











Compute gradients using autodiff and solve with gradient ascent



SuperTrack: Motion Tracking for Physically Simulated Characters Using Supervised Learning [Fussell et al. 2021]





A1 Quadruped Walking

UR5 Multi-Object Visual Pick Place



XArm Visual Pick and Place



Sphero Ollie Visual Navigation

DayDreamer: World Models for Physical Robot Learning [Wu et al. 2022]



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Model Exploitation

ALGORITHM: DYNA

- 1: $\pi^0 \leftarrow$ initialize policy
- 2: $\mathcal{D} \leftarrow \{\emptyset\}$ initialize dataset

Fit dynamics model:

- 3: for iteration k = 0, ..., n 1 do
- Sample trajectory τ according to $\pi^k(\mathbf{a}|\mathbf{s})$ 4:
- Add transitions to dataset $\mathcal{D} = \mathcal{D} \cup \{(\mathbf{s}_i, \mathbf{a}_i, \mathbf{s}'_i)\}$ 5:

6: Fit dynamics model:

$$f = \arg \max_{f} \mathbb{E}_{(\mathbf{s}, \mathbf{a}, \mathbf{s}') \sim \mathcal{D}} \left[\log f(\mathbf{s}' | \mathbf{s}, \mathbf{a}) \right]$$

 $\pi^{k+1} \leftarrow \text{train policy by simulating rollouts with } f(\mathbf{s}'|\mathbf{s}, \mathbf{a})$ 7: 8: end for

9: return π^n

Dyna, an Integrated Architecture for Learning, Planning, and Reacting [Sutton 1991]

Aleatoric (Statistical Uncertainty)



Epistemic (Model Uncertainty)



Aleatoric (Statistical Uncertainty)





Aleatoric (Statistical Uncertainty)



Epistemic (Model Uncertainty)





Aleatoric (Statistical Uncertainty)





Policy can exploit model uncertainty

• Can we estimate the model uncertainty?



- Can we estimate the model uncertainty?
- Bayesian inference:





- Can we estimate the model uncertainty?
- Bayesian inference:





High Likelihood

- Can we estimate the model uncertainty?
- Bayesian inference:





- Can we estimate the model uncertainty?
- Bayesian inference:

$$p(f|\mathcal{D}) = \frac{p(f,\mathcal{D})}{p(\mathcal{D})}$$

- Can we estimate the model uncertainty?
- Bayesian inference:

$$\begin{split} p(f|\mathcal{D}) &= \frac{p(f,\mathcal{D})}{p(\mathcal{D})} \\ &= \frac{p(\mathcal{D}|f)p(f)}{p(\mathcal{D})} \end{split}$$

Supervised Learning

$$\underset{f}{\arg \max} \ \log p(f|\mathcal{D}) = \underset{f}{\arg \max} \ \log \frac{p(\mathcal{D}|f)p(f)}{p(\mathcal{D})}$$

Supervised Learning

$$\arg \max_{f} \frac{\log p(f|\mathcal{D})}{\int} = \arg \max_{f} \frac{\log \frac{p(\mathcal{D}|f)p(f)}{p(\mathcal{D})}}{\int}$$
$$= \arg \max_{f} \frac{\log p(\mathcal{D}|f) + \log p(f) - \log p(\mathcal{D})}{\int}$$
$$I$$

Posterior Likelihood Prior Constant

Supervised Learning

$$\arg \max_{f} \underline{\log p(f|\mathcal{D})} = \arg \max_{f} \frac{\log \mathcal{D}(f)p(f)}{p(\mathcal{D})}$$
$$= \arg \max_{f} \frac{\log p(\mathcal{D}|f) + \log p(f) - \log p(\mathcal{D})}{\mathsf{Likelihood}}$$
$$\underbrace{\bigvee_{f}}{\mathsf{Maximum Likelihood}}$$
$$\arg \max_{f} \mathbb{E}_{(\mathbf{s}, \mathbf{a}, \mathbf{s}') \sim \mathcal{D}} \left[\log f(\mathbf{s}'|\mathbf{s}, \mathbf{a})\right]$$
Supervised Learning



Supervised Learning



Uncertainty Estimation

- Maximum likelihood only gives a *point-wise* approximation of the posterior
- To estimate model uncertainty, need to approximate the *full* posterior



Ensemble

Ensemble



Ensemble

- Approximate posterior with ensemble
- Models should be consistent under the data distribution



Ensemble

- Approximate posterior with ensemble
- Models should be consistent under the data distribution
- Models will hopefully disagree on out-of-distribution samples



Bootstrapping

- Split dataset into subsets
- Train a separate model for each subset





Bootstrapping

- Split dataset into subsets
- Train a separate model for each subset



In practice:

- Initialize models with different random parameters
- Train all models using the same dataset
- Stochasticity from SGD leads to diverse models

• Sample random model for every transition



• Sample random model for every transition



• Sample random model for every transition



• Sample random model for every transition



• Sample random model for every transition



- Sample random model for every transition
- Penalize policy for model disagreement

 $r(\mathbf{s}, \mathbf{a}, \mathbf{s'})$

- Sample random model for every transition
- Penalize policy for model disagreement

$$r_p(\mathbf{s}, \mathbf{a}, \mathbf{s'}) = \begin{cases} -\kappa & \text{if } d(\mathbf{s}, \mathbf{a}) > \alpha \\ r(\mathbf{s}, \mathbf{a}, \mathbf{s'}) & \text{otherwise} \end{cases}$$

- Sample random model for every transition
- Penalize policy for model disagreement

$$r_p(\mathbf{s}, \mathbf{a}, \mathbf{s'}) = \begin{cases} -\kappa & \text{if } d(\mathbf{s}, \mathbf{a}) > \alpha \\ r(\mathbf{s}, \mathbf{a}, \mathbf{s'}) & \text{otherwise} \end{cases}$$

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Model disagreement:

$$d(\mathbf{s}, \mathbf{a}) = \max_{i,j} D\left(f_i(\cdot|\mathbf{s}, \mathbf{a}), f_j(\cdot|\mathbf{s}, \mathbf{a})\right)$$

- Sample random model for every transition
- Penalize policy for model disagreement
- Termination based on disagreement



Uncertainty Estimation

- Ensembles
- Bayesian Neural Networks
- Dropout
- Normalized Maximum Likelihood
- Test Time Augmentation
- Etc...

Model-Predictive Control

Model-Based Policy Learning



Q-Learning











• Use dynamics model to predict expected return of every action

$$\underset{\mathbf{a}_{0:k}}{\operatorname{arg max}} \ \mathbb{E}_{\tau \sim f(\tau | \mathbf{s}_0 = \mathbf{s}, \mathbf{a}_{0:k})} \left[R(\tau) \right]$$



• Use dynamics model to predict expected return of every action

$$\underset{\mathbf{a}_{0:k}}{\operatorname{arg max}} \mathbb{E}_{\tau \sim f(\tau | \mathbf{s}_0 = \mathbf{s}, \mathbf{a}_{0:k})} [R(\tau)]$$

• Apply optimal action sequence $\mathbf{a}^*_{0:k}$ in real environment



Drift



Drift



Drift



Drift



Drift



Drift



Drift


• Use dynamics model to predict expected return of every action

$$\begin{array}{c} \arg\max \ \mathbb{E}_{\tau \sim f(\tau | \mathbf{s}_0 = \mathbf{s}, \mathbf{a}_{0:k})} \left[R(\tau) \right] \\ \bullet \text{ Apply optimal action sequence } \mathbf{a}_{0:k}^* \text{ in real environment} \end{array}$$

- Model Predictive Control (MPC)
 - Apply only the first action in the real environment
 - Replan every timestep

$$\overbrace{r_0}^{\mathbf{s}_0} \overbrace{r_1}^{\mathbf{s}_1} \overbrace{r_1}^{\mathbf{s}_2} \overbrace{\mathbf{s}_k}^{\mathbf{s}_k} \overbrace{\mathbf{s}_{k+1}}^{\mathbf{s}_k}$$

Drift



Drift



Drift



Drift



Drift



Drift



Drift



(Closed-Loop Control)

• How to solve optimization problem every timestep?

$$\underset{\mathbf{a}_{0:k}}{\operatorname{arg max}} \ \mathbb{E}_{\tau \sim f(\tau | \mathbf{s}_0 = \mathbf{s}, \mathbf{a}_{0:k})} \left[R(\tau) \right]$$

- Black-Box Optimization
 - CEM, random shooting, etc.
- If differentiable model and reward function, use gradient ascent
- Can incorporate other model-based RL improvements
 - Uncertainty estimation, ensembles, etc.





Learning Latent Dynamics for Planning from Pixels [Hafner et al. 2019]

MPC



Deep Dynamics Models for Learning Dexterous Manipulation [Nagabandi et al. 2019]

MPC



Deep Dynamics Models for Learning Dexterous Manipulation [Nagabandi et al. 2019]

Policy Learning

- Learn model + policy
- Runtime policy inference is fast
- Policy is task-specific
- Typically better asymptotic performance

Online Planning

- Learn model
- Runtime planning can be slow
- Model can be task-agnostic
- May need many samples during online planning to find good plans

Summary

- Model-Based RL
- DYNA
- Model Representations
- Uncertainty Estimation
- MPC